

# Numerical Simulation Tools and Methods used at ETP

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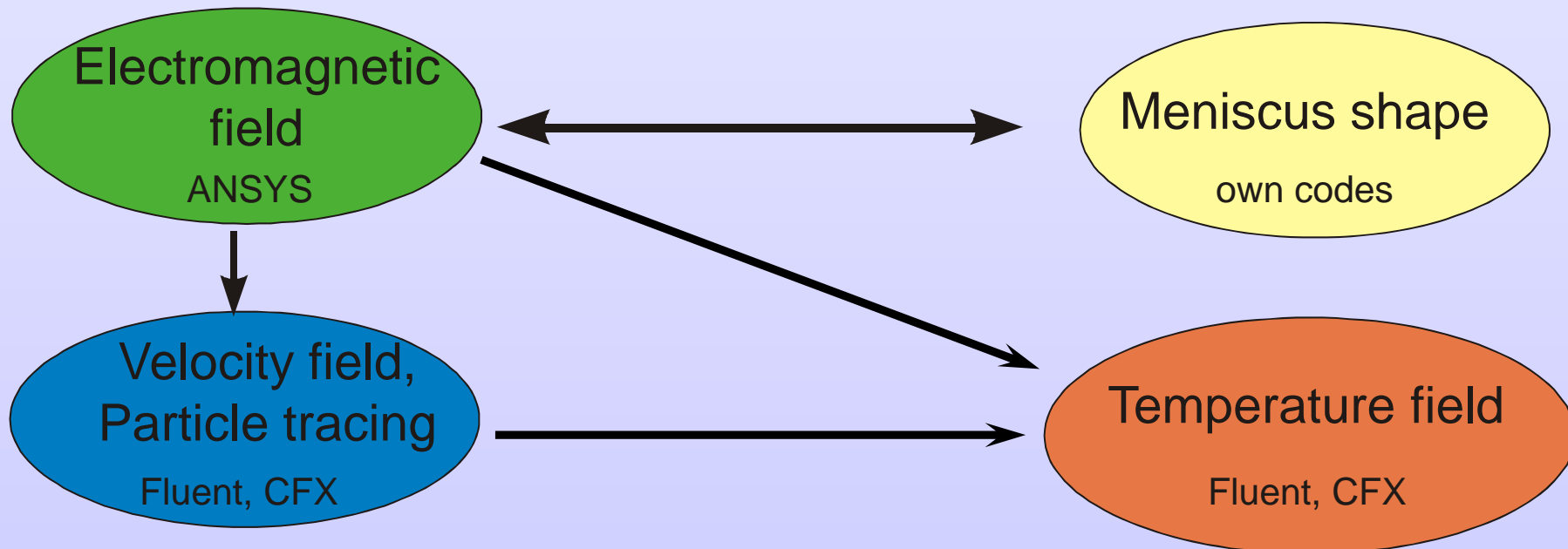
## Content

- **Numerical simulation of melt flows in induction furnaces**
- **Analysis and design of complex induction heating processes**
- **Simulation of complex 3D temperature fields in systems for crystal growing of photovoltaic cells**
- **Optimal design and process control of induction heated systems using mathematical optimization**
- **Conclusion and future challenges**

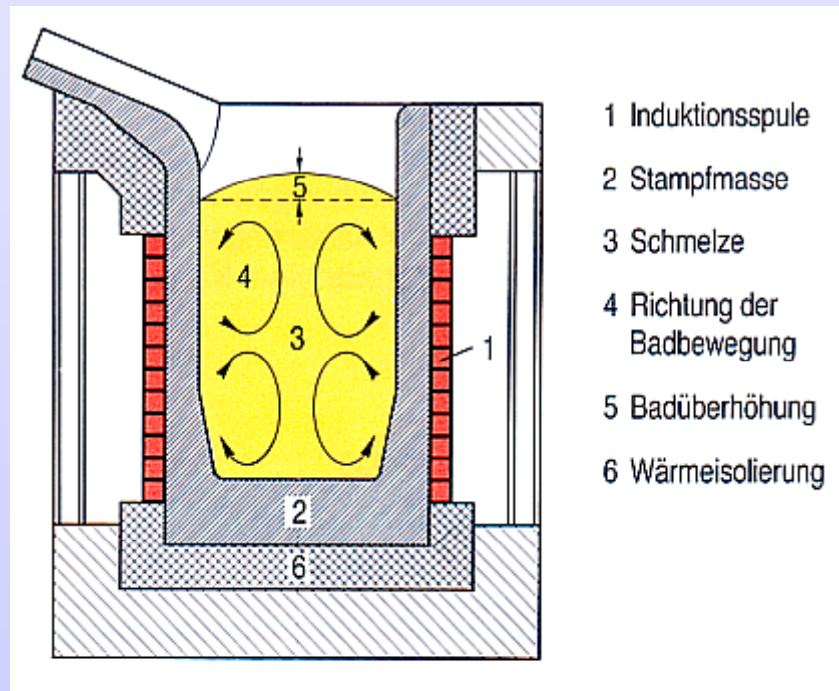
## Numerical simulation of melt flows in induction furnaces

- Tools and general aspects
- Induction crucible furnace
- Induction channel furnace
- Induction skull melting

## Physical correlations in induction furnaces and used tools

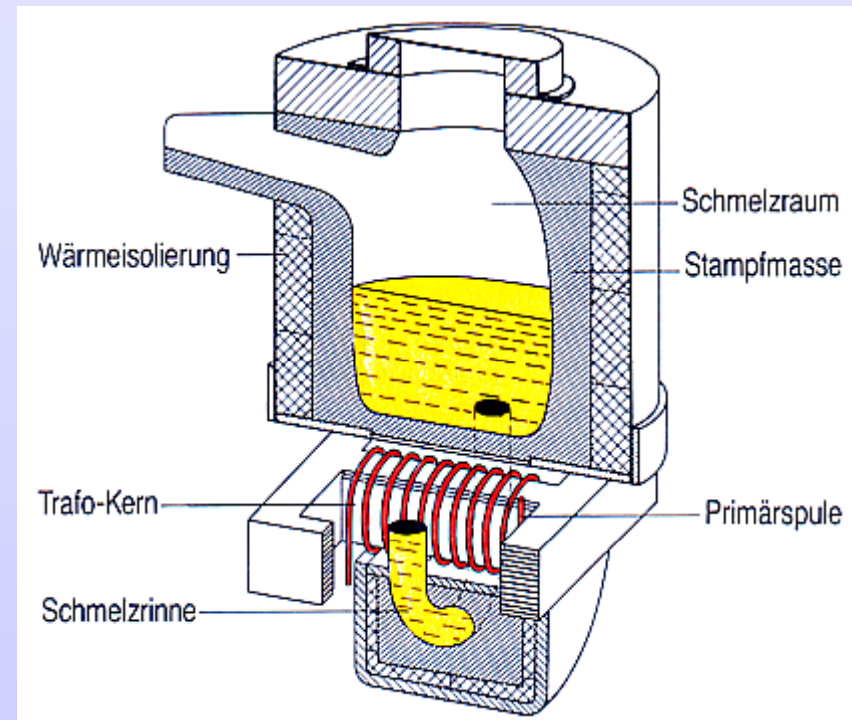


## Induction crucible furnace



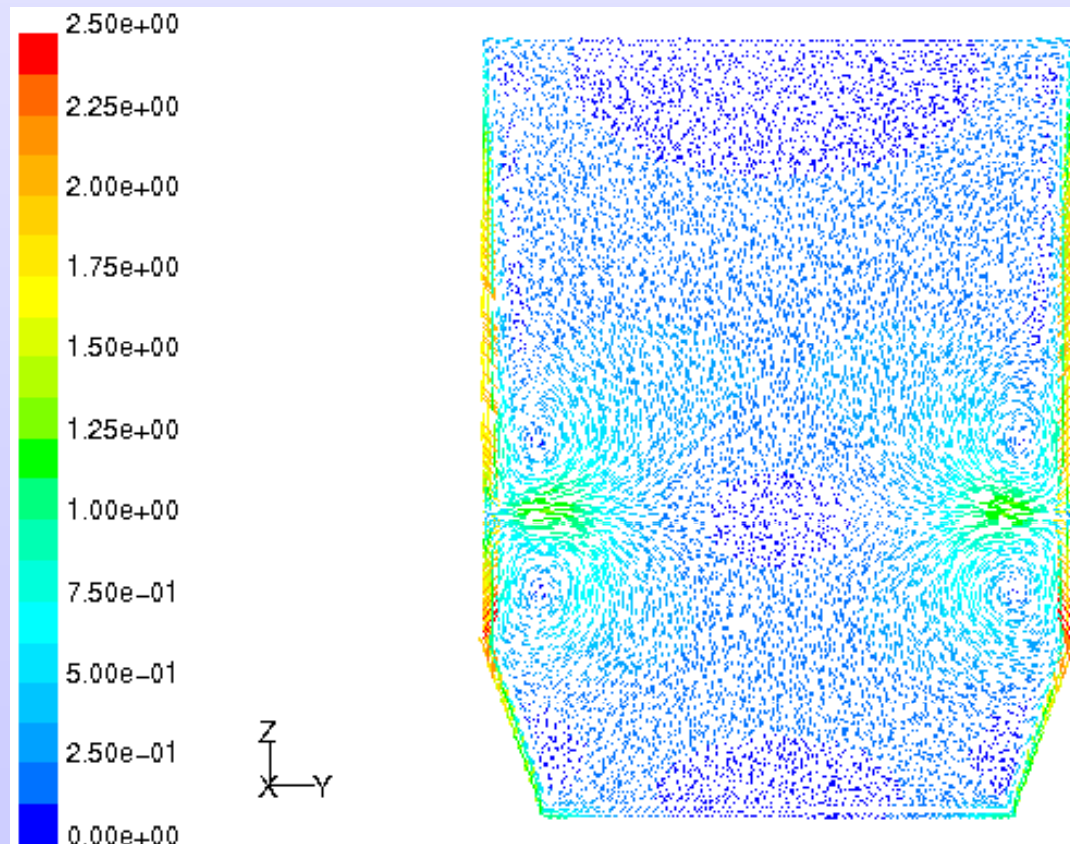
- Used mainly for melting
- Medium high efficiency
- Operating frequency: 50 ... 1000 Hz

## Induction channel furnace



- Used mainly for holding and pouring
- High efficiency
- Operating frequency: 50 Hz, 60 Hz

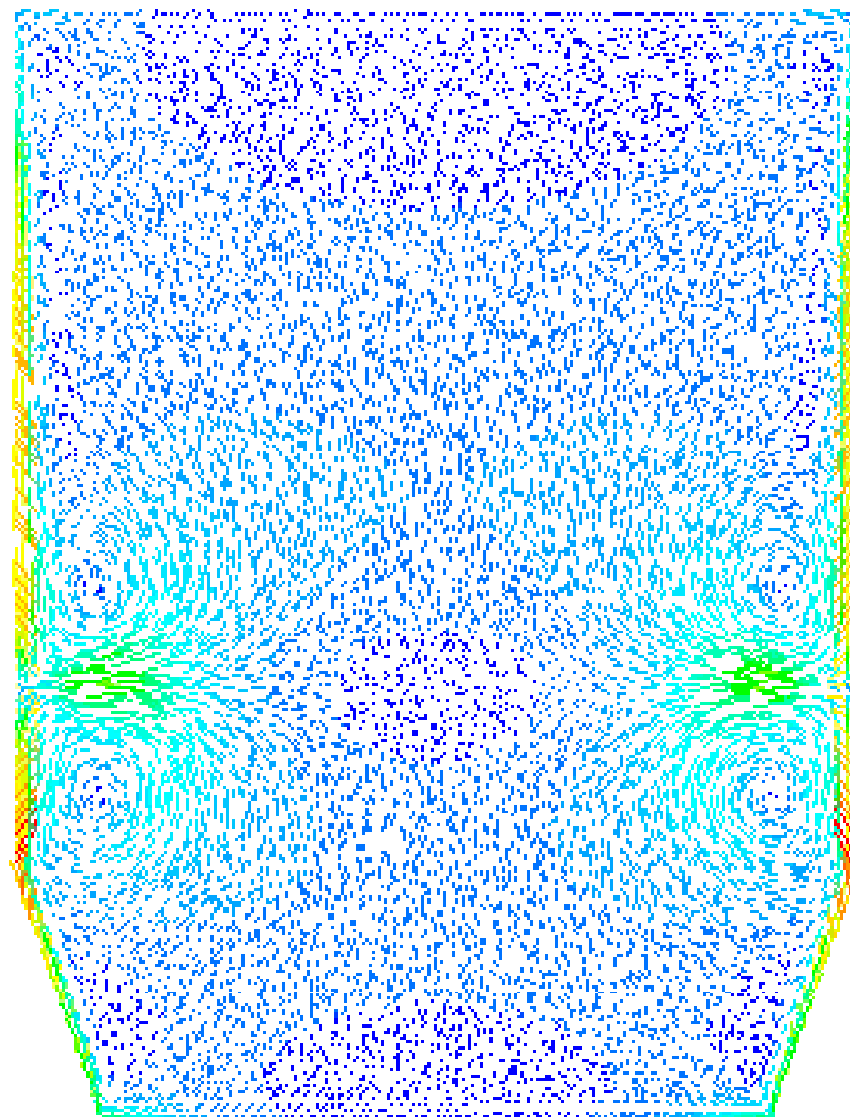
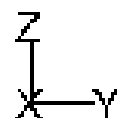
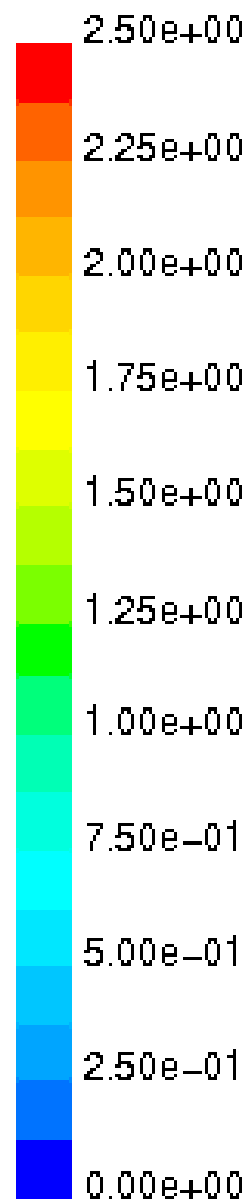
## Transient 3D-Large Eddy Simulation of the melt flow in an industrial used induction crucible furnace



Medium frequency  
induction crucible  
furnace:

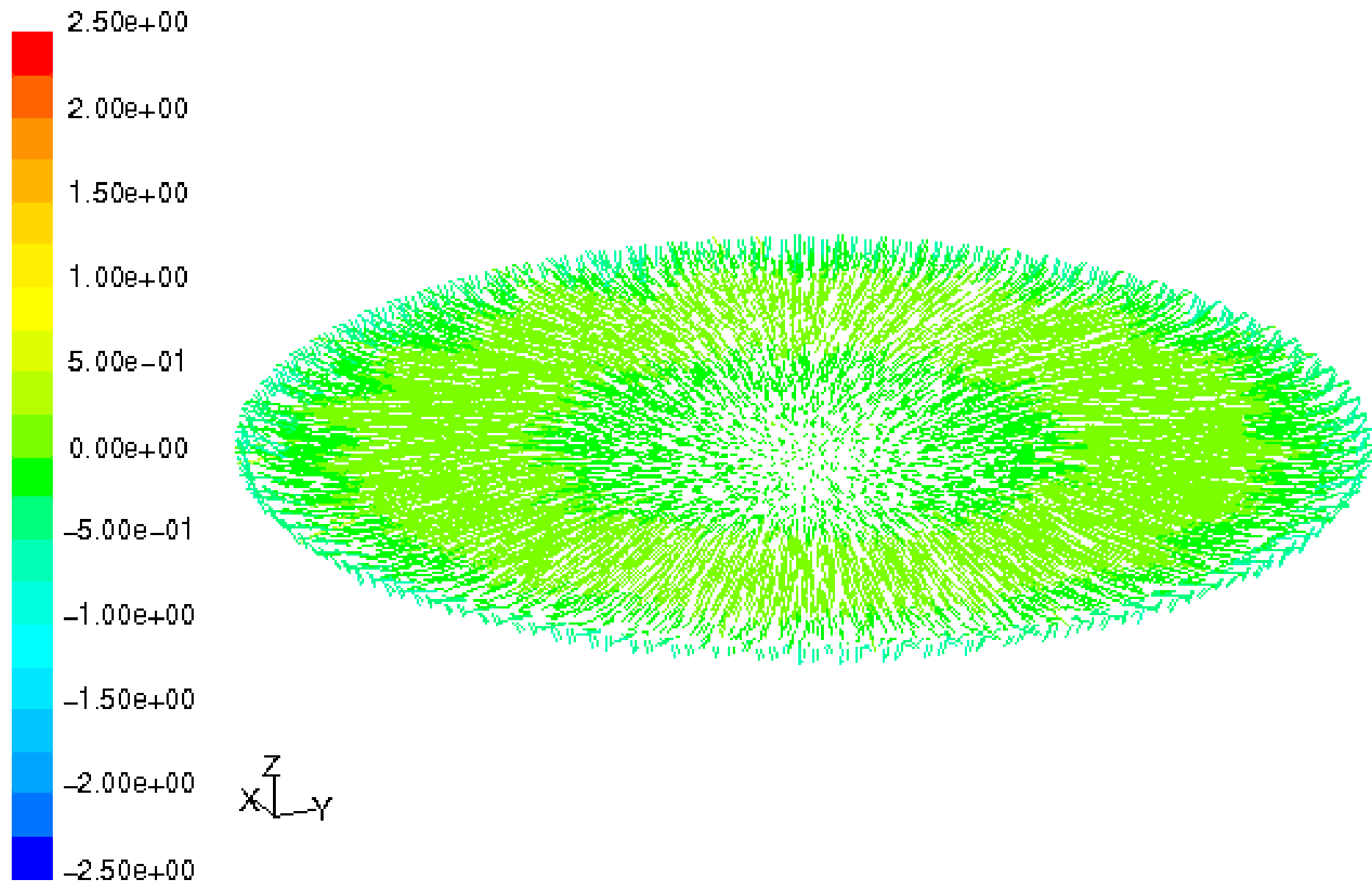
- 12 t grey cast iron
- power 9,3 MW
- frequency 230 Hz

crucible diameter: 1,20 m  
crucible height: 1,30 m



Velocity Vectors Colored By plane-velocity (Time=1.2600e+00)

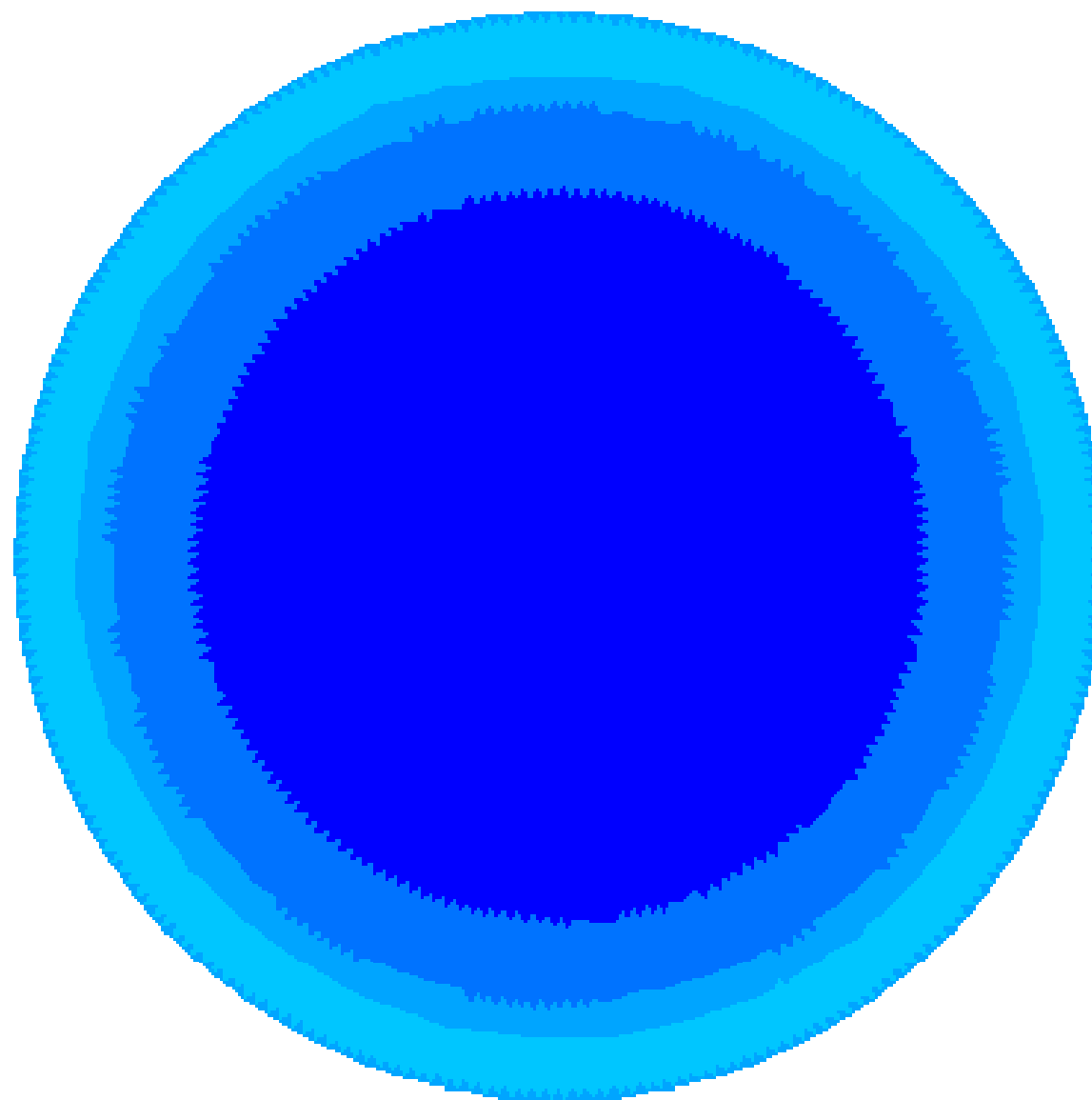
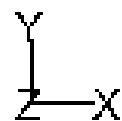
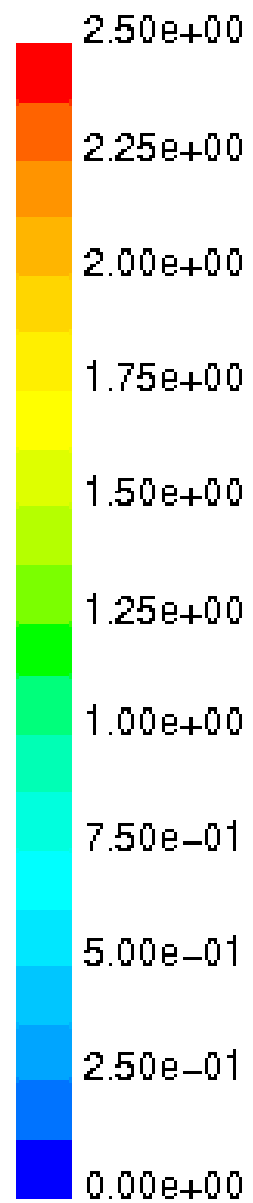
Aug 13, 2001  
FLUENT 5.4 (3d, segregated, LES, unsteady)



Velocity Vectors Colored By Axial Velocity ( m/s) (Time=1.6600e+00)

Aug 13, 2001

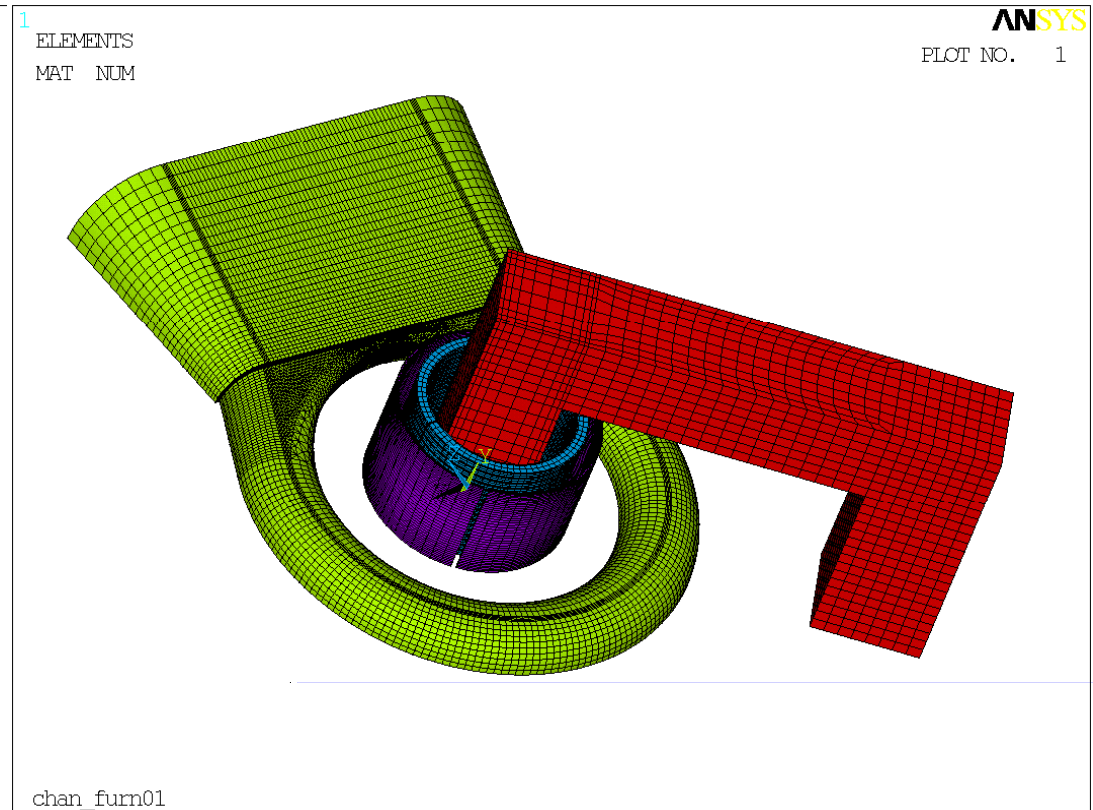
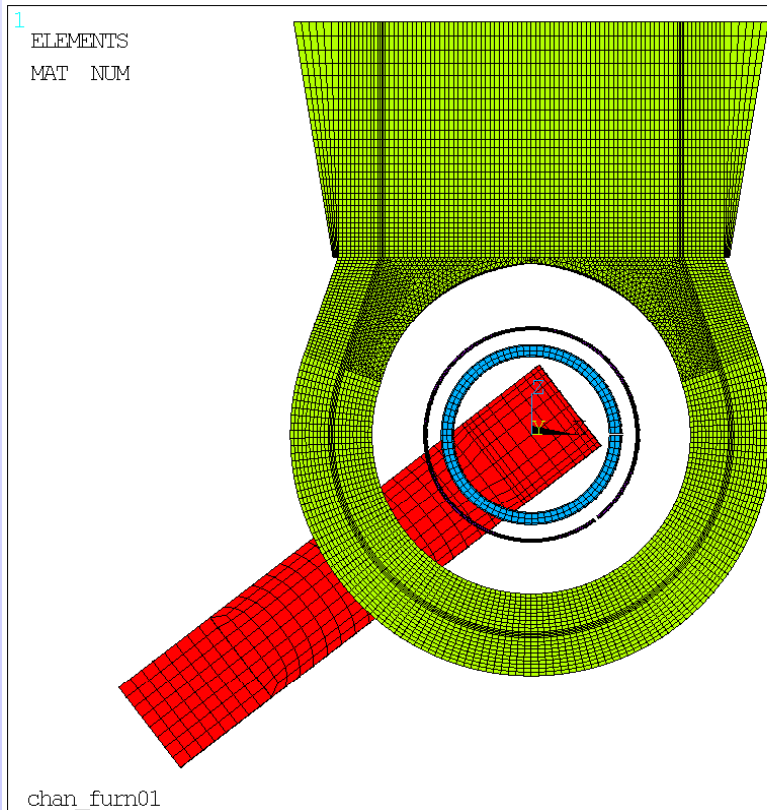
FLUENT 5.4 (3d, segregated, LES, unsteady)



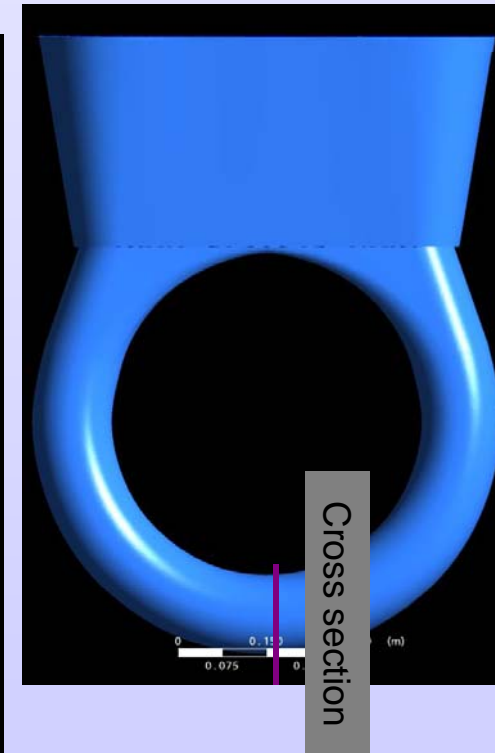
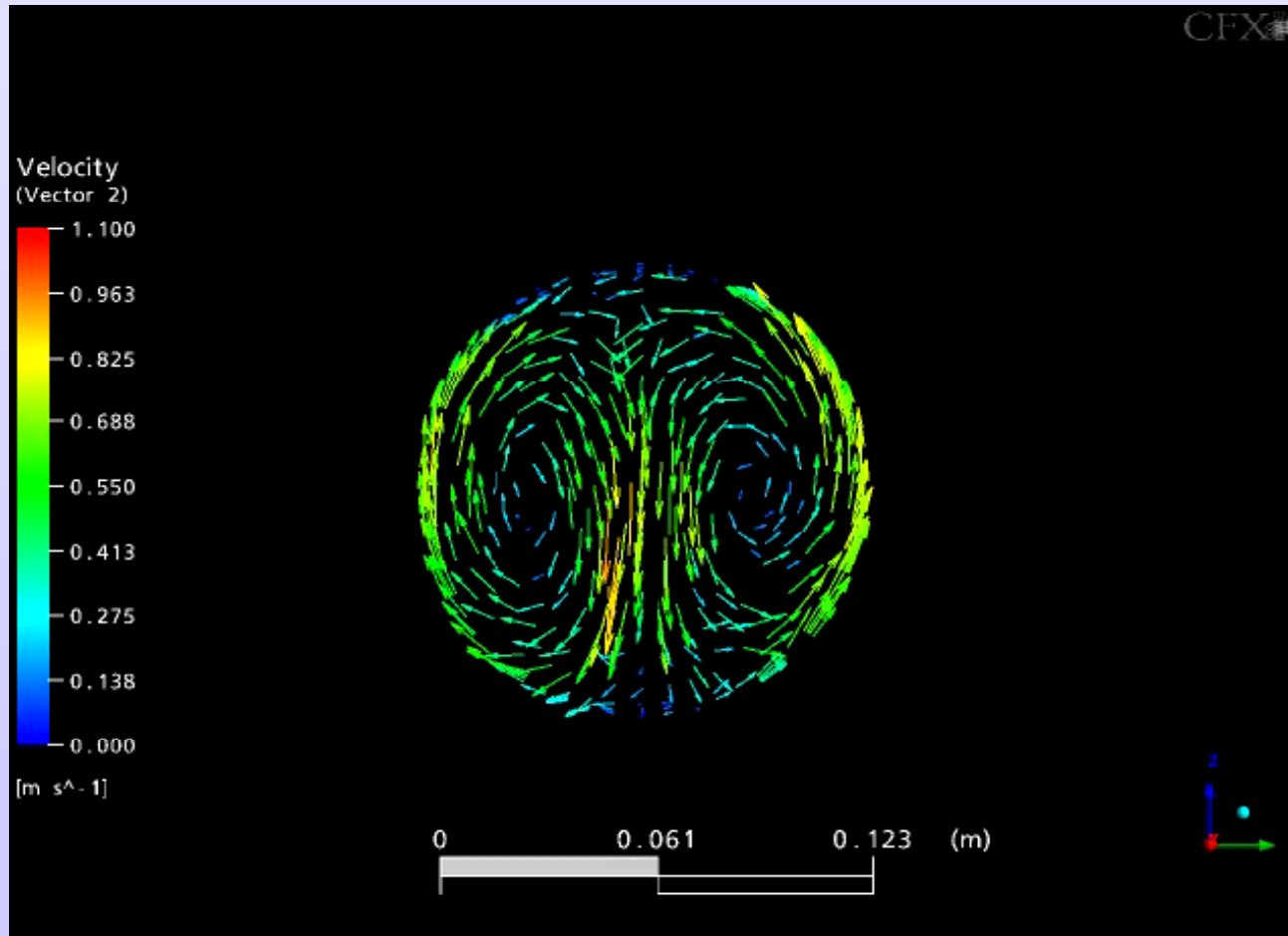
Contours of Velocity Magnitude (m/s) (Time=1.2600e+00)

Aug 13, 2001  
FLUENT 5.4 (3d, segregated, LES, unsteady)

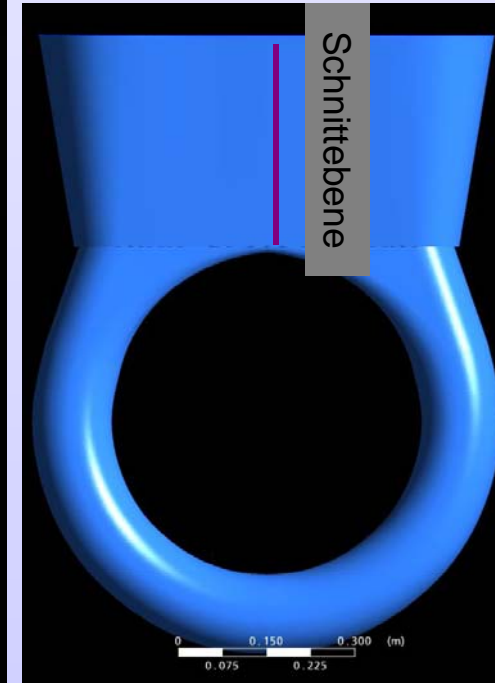
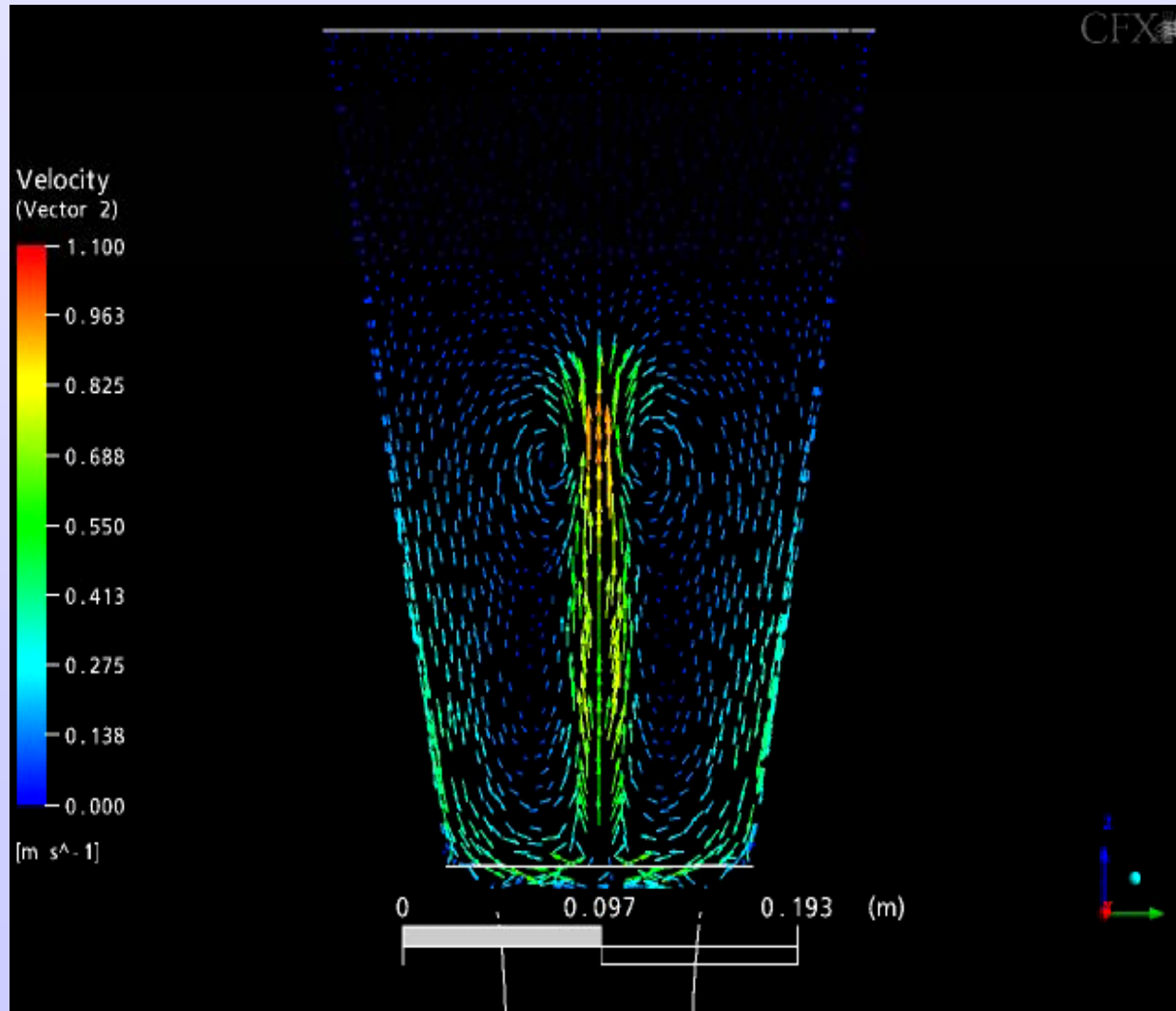
# 3D-Simulation model for electromagnetic calculation of the channel inductor (power density and electromagnetic force density)



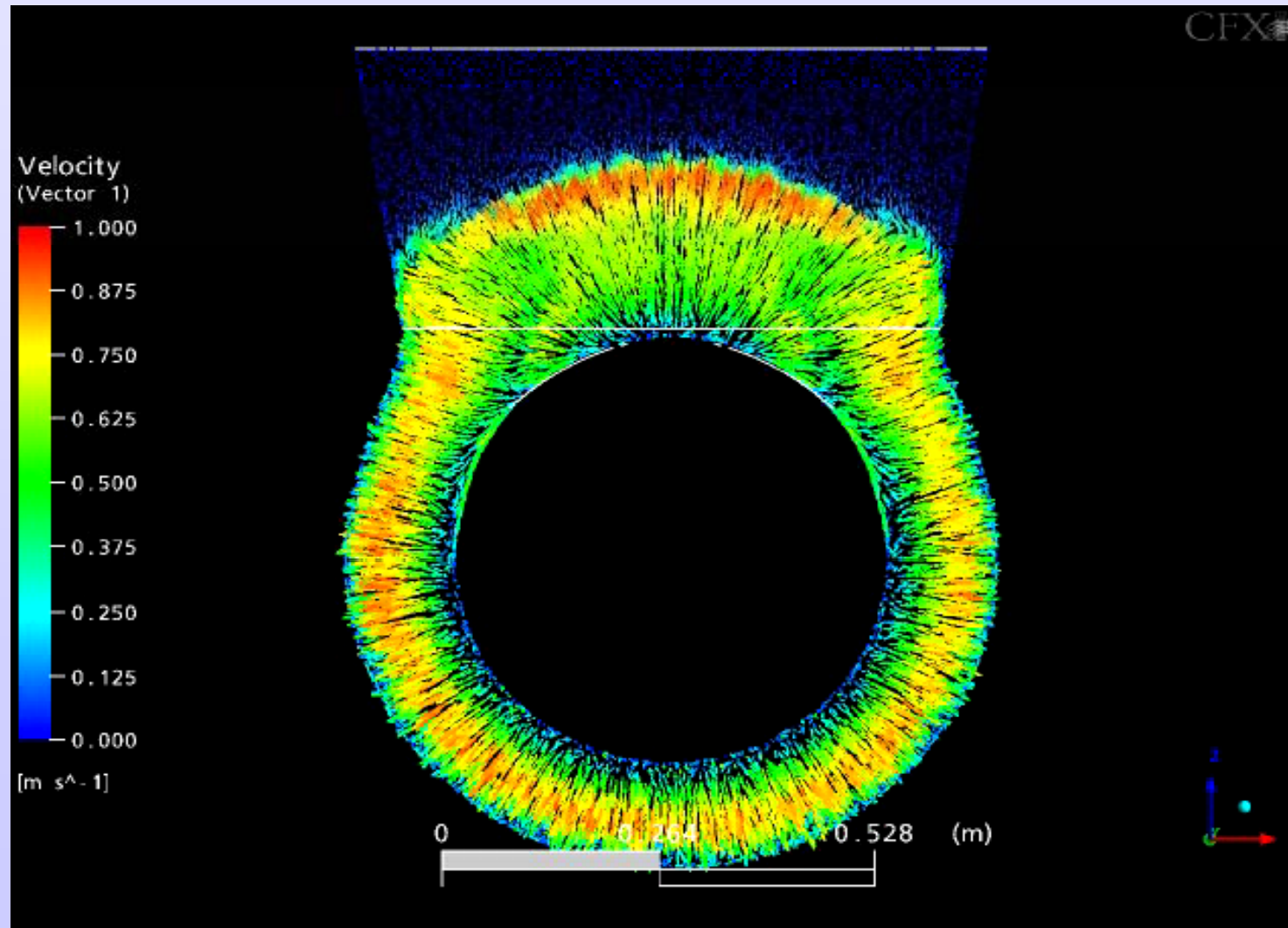
# 3D transient simulation of the melt flow in cross section of the channel (LES model)



# 3D transient simulation of the melt flow in the bath (LES model)

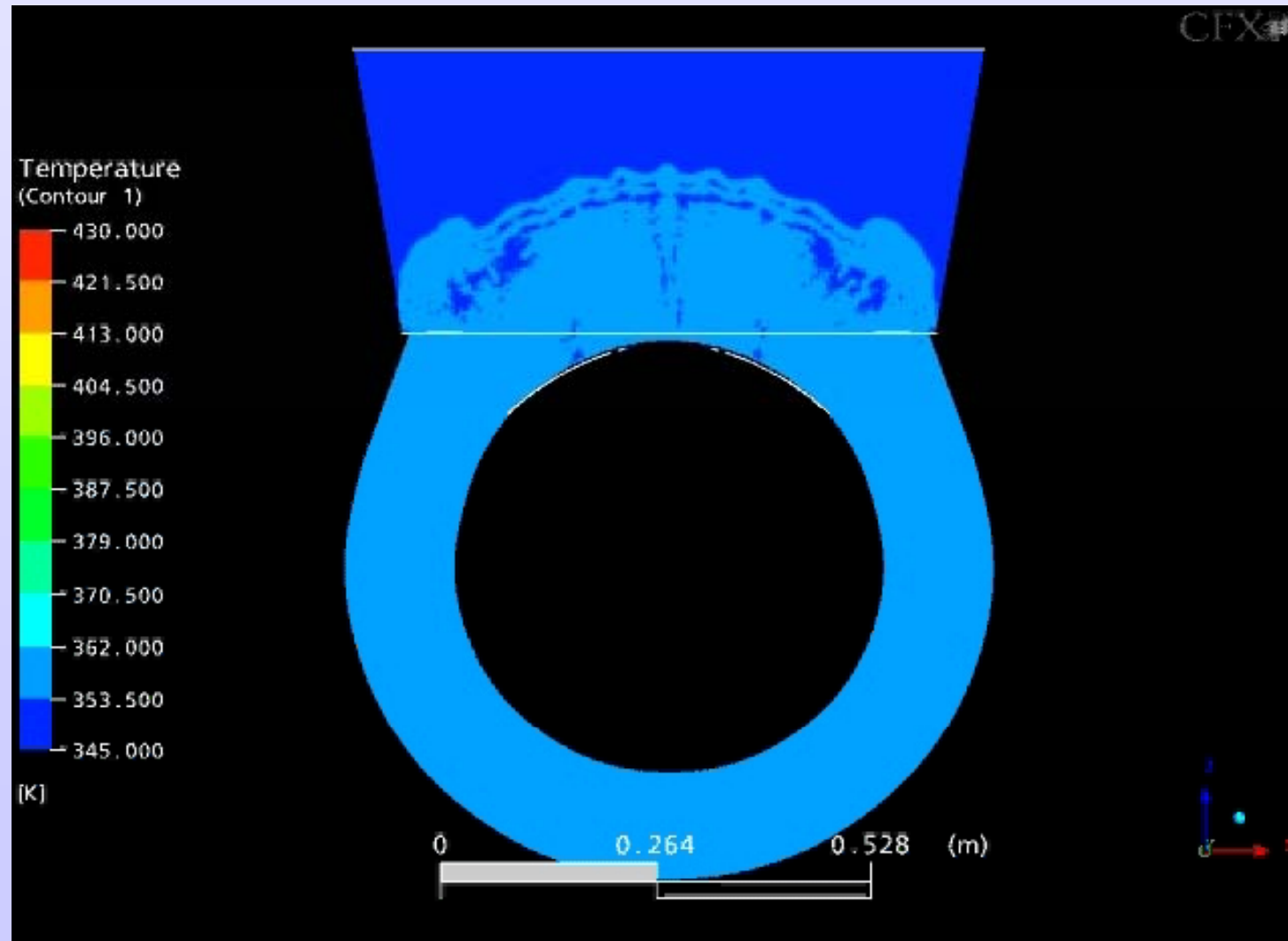


## 3D transient simulation of the melt flow in the channel (LES model)

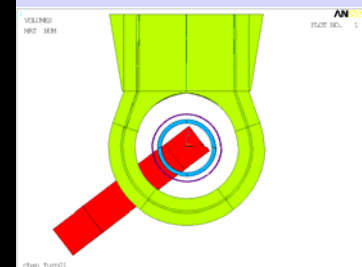


$v_0 = 0$  m/s

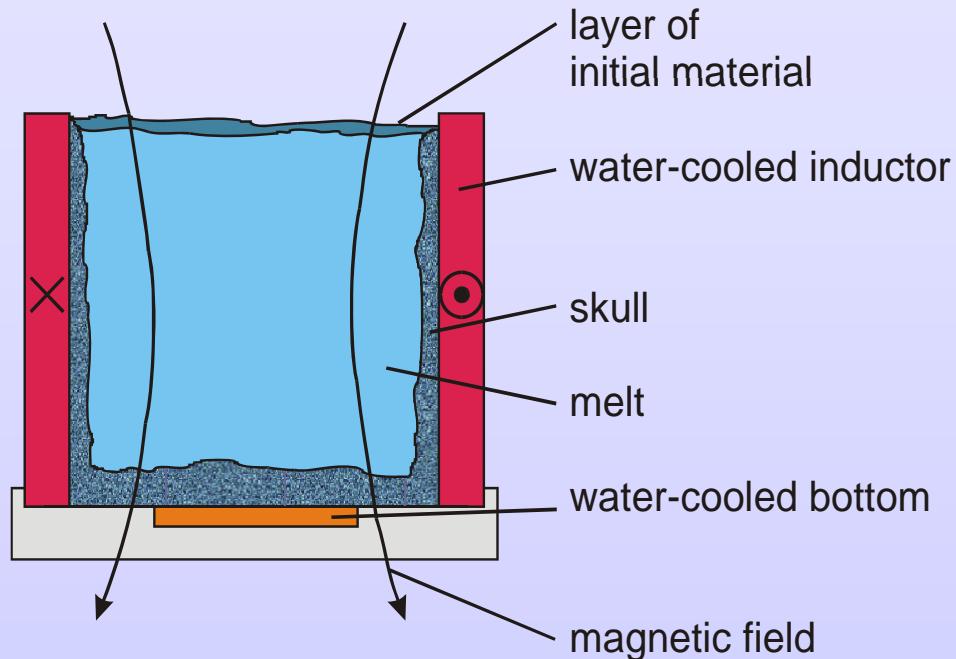
## temperature distribution in the channel (LES model)



$$T_0 = 80^\circ\text{C}$$



## Principle of induction skull melting technology



Intensive cooling of inductor and bottom

- formation of a skull
- skull protects against impurities

### Advantages of induction skull melting

High process temperatures

High power density

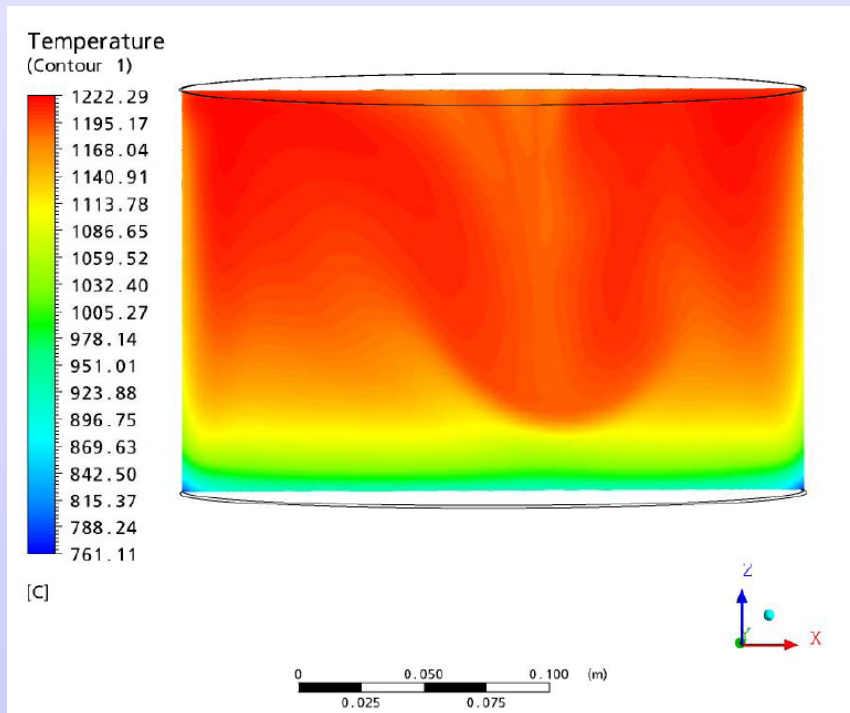
High purity of the melt and the final product

High efficiency

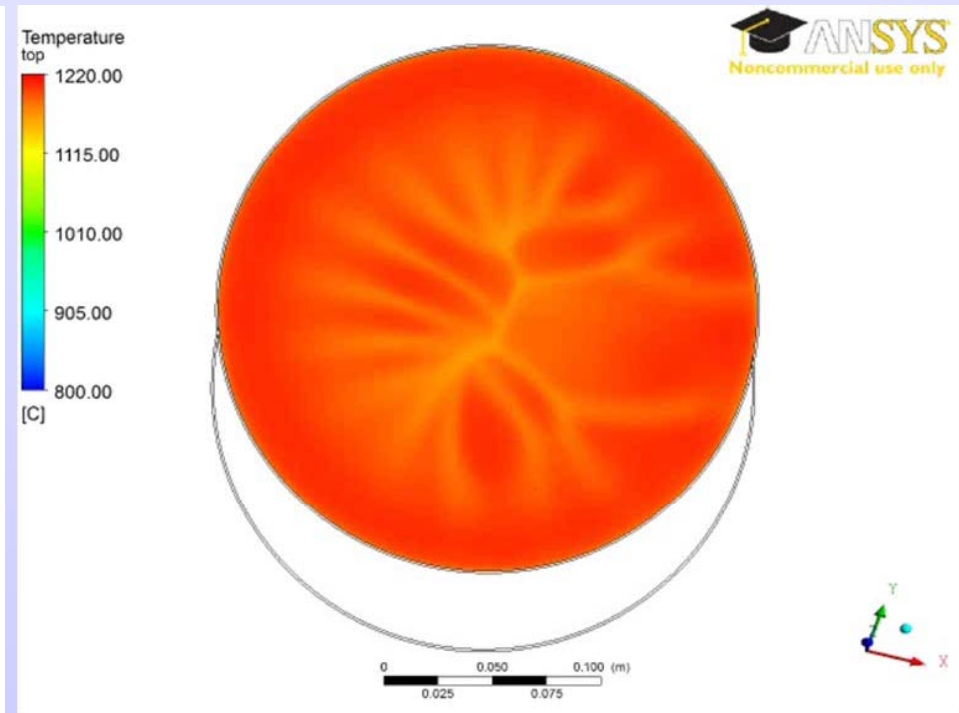
Process can be realized in different gas atmospheres or in vacuum

Compact melting equipment

Glass with medium electrical conductivity, medium viscosity



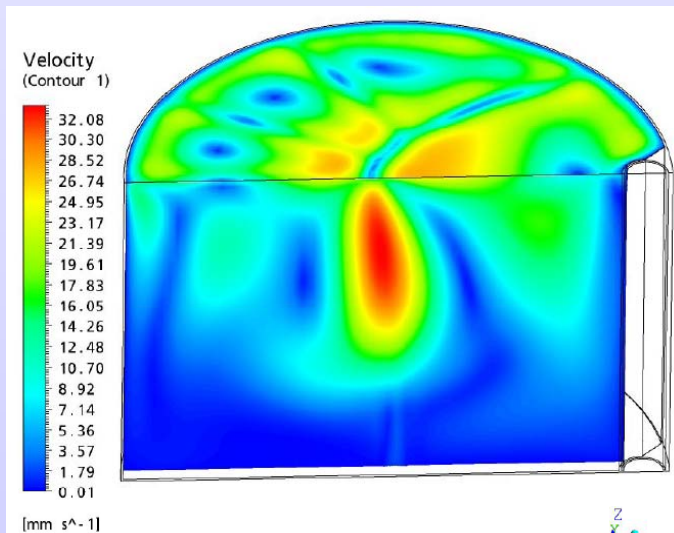
The temperature distribution is divided in 3 areas with different temperature levels.



The surface shows pattern of bifurcated channels created by Marangoni convection.

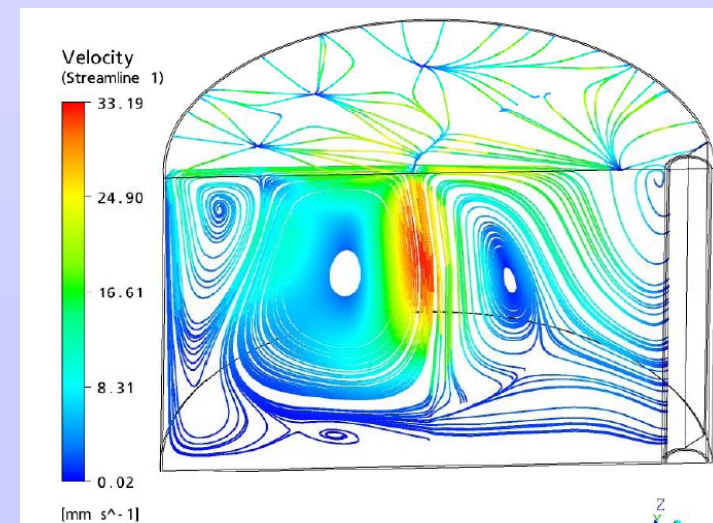
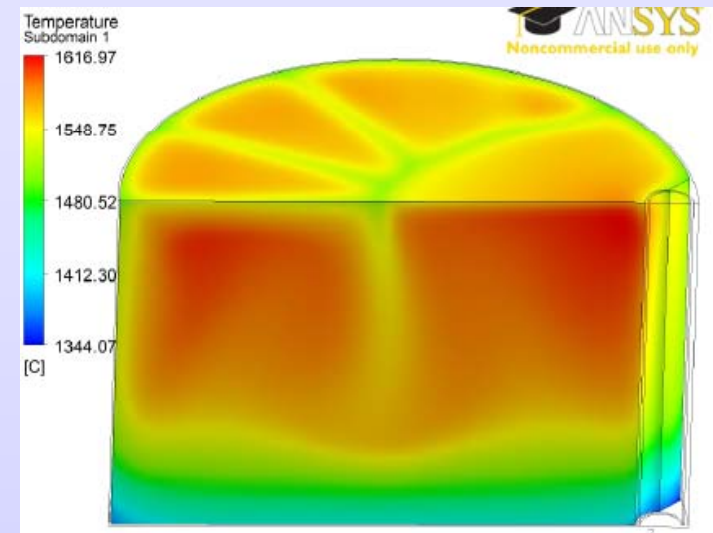
# Hydrodynamic thermal simulation (Glass 2)

Glass with high electrical conductivity, high viscosity



Also channels at the melt surface,  
but less and without bifurcation

Stream lines with typical  
inner and outer flow eddies

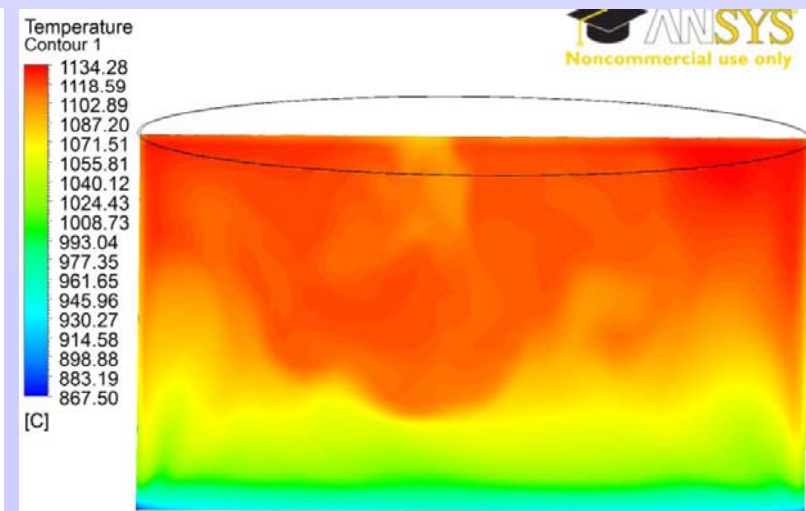
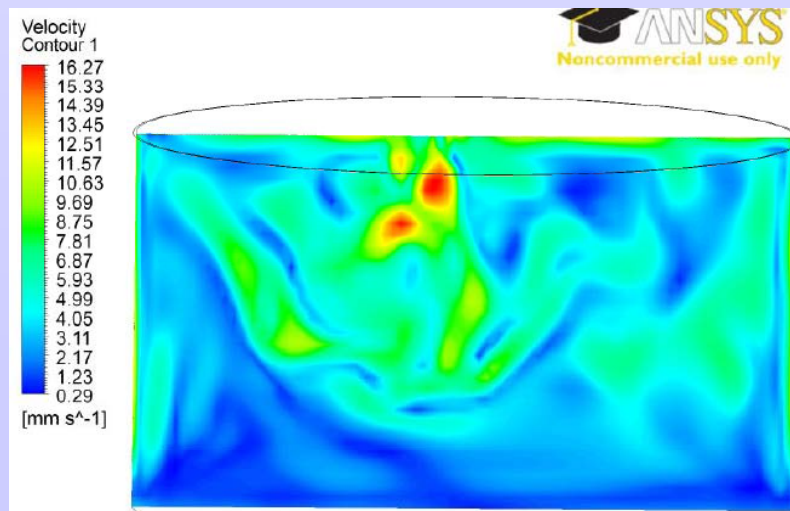
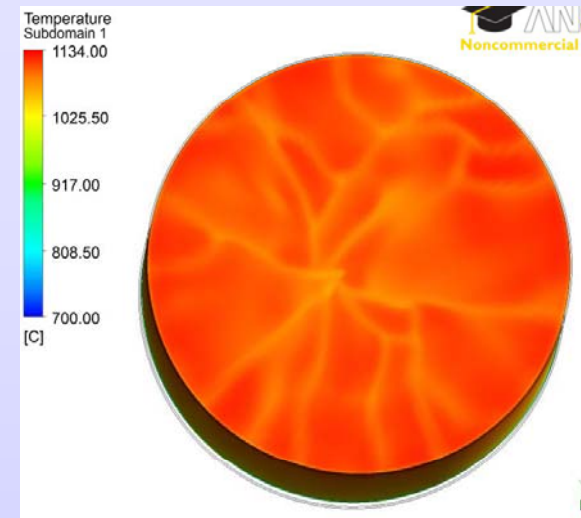


# Hydrodynamic thermal simulation (Glass 3)

Glass with medium electrical conductivity,  
medium viscosity

Chaotic distribution of channels at the melt surface

Higher turbulence due to lower viscosity



## Analysis and design of complex induction heating processes

- Tools and general aspects
- Surface hardening of worm gears

# Tools for modelling of induction heating processes

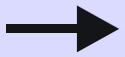
Engineering tools



2D-program HIHTEC  
(BEM)

- electromagnetic
- ➔ integral parameters
- preliminary investigation, optimization

Special programs



3D-program package HIHTEC  
(BEM, FDM)

- electromagnetic, thermal
- ➔ integral + distributed parameters
- parametrical studying, mathem. optimization

Universal commercial packages



3D-program package ANSYS  
(FEM)

- electromagnetic, thermal, mechanical
- ➔ integral + distributed parameters
- verification, complicated systems, partial optimization

combined tools

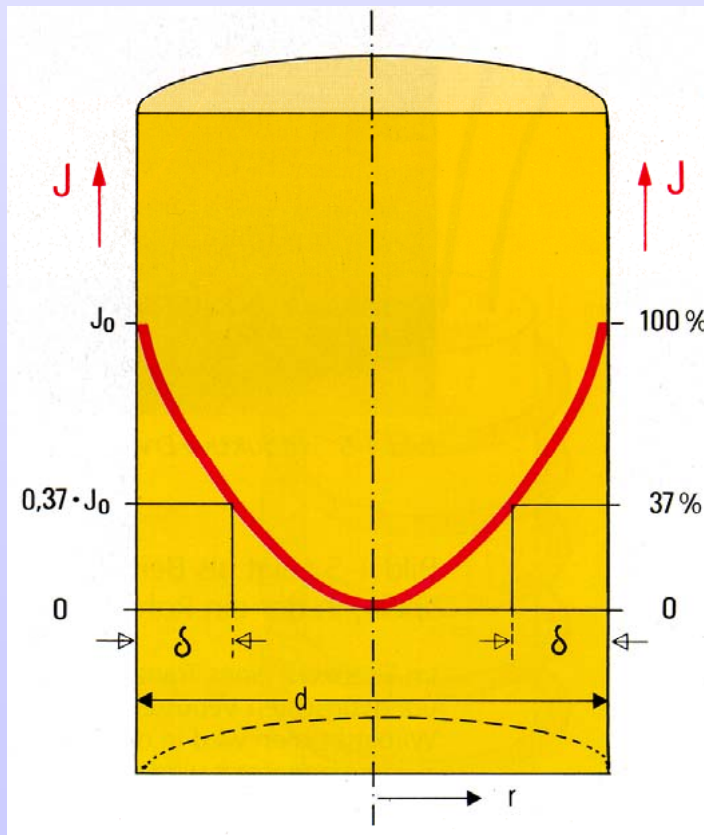


Combined 3D-programs  
(BEM, FDM, FEM)

- electromagnetic, thermal
- ➔ distributed parameters
- nonlinear systems

## Skin effect

Current density distribution in a cylindrical work-piece (approximation)



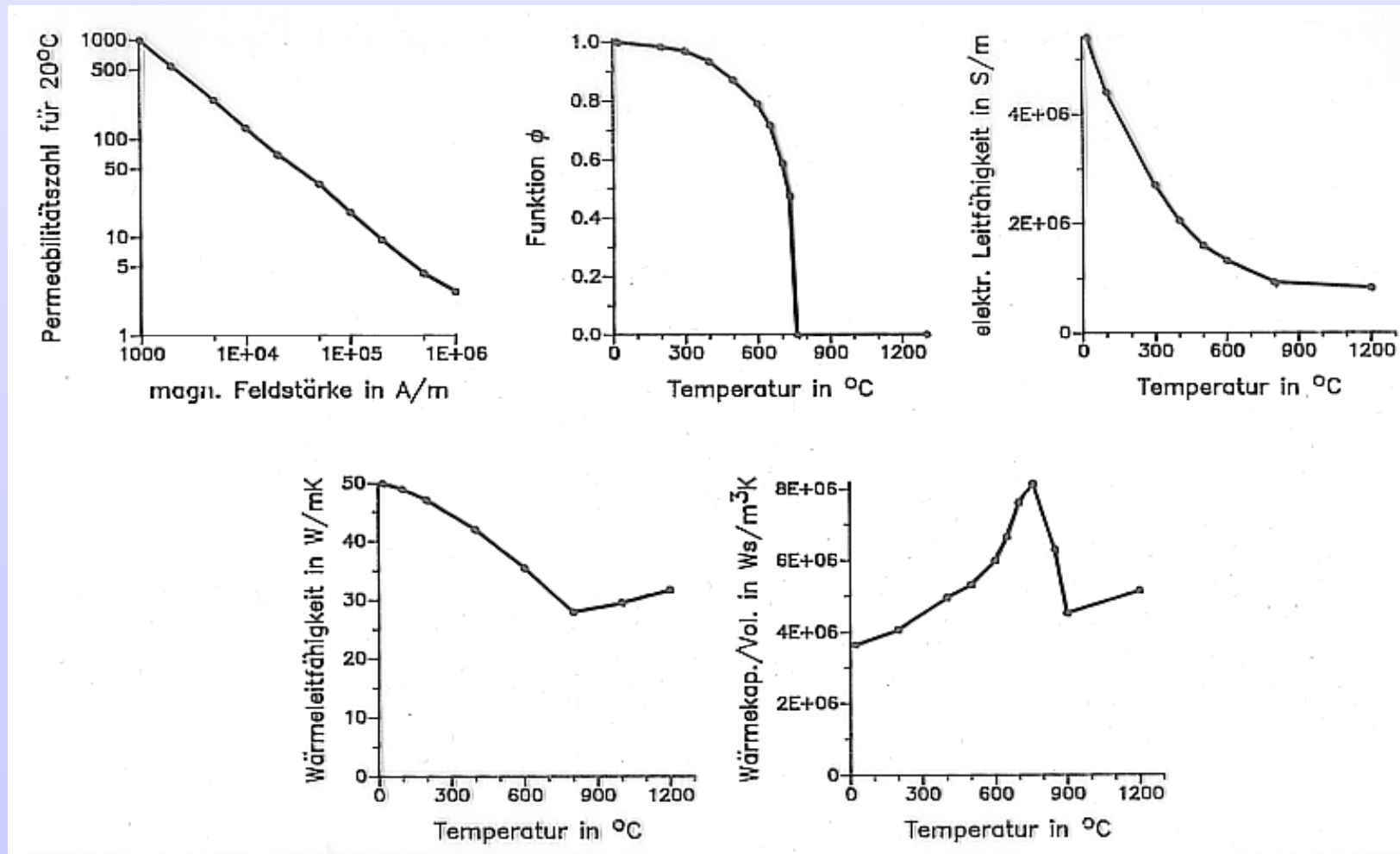
Electromagnetic penetration depth

$$\delta = \sqrt{\frac{\rho}{\pi \cdot f \cdot \mu}}$$

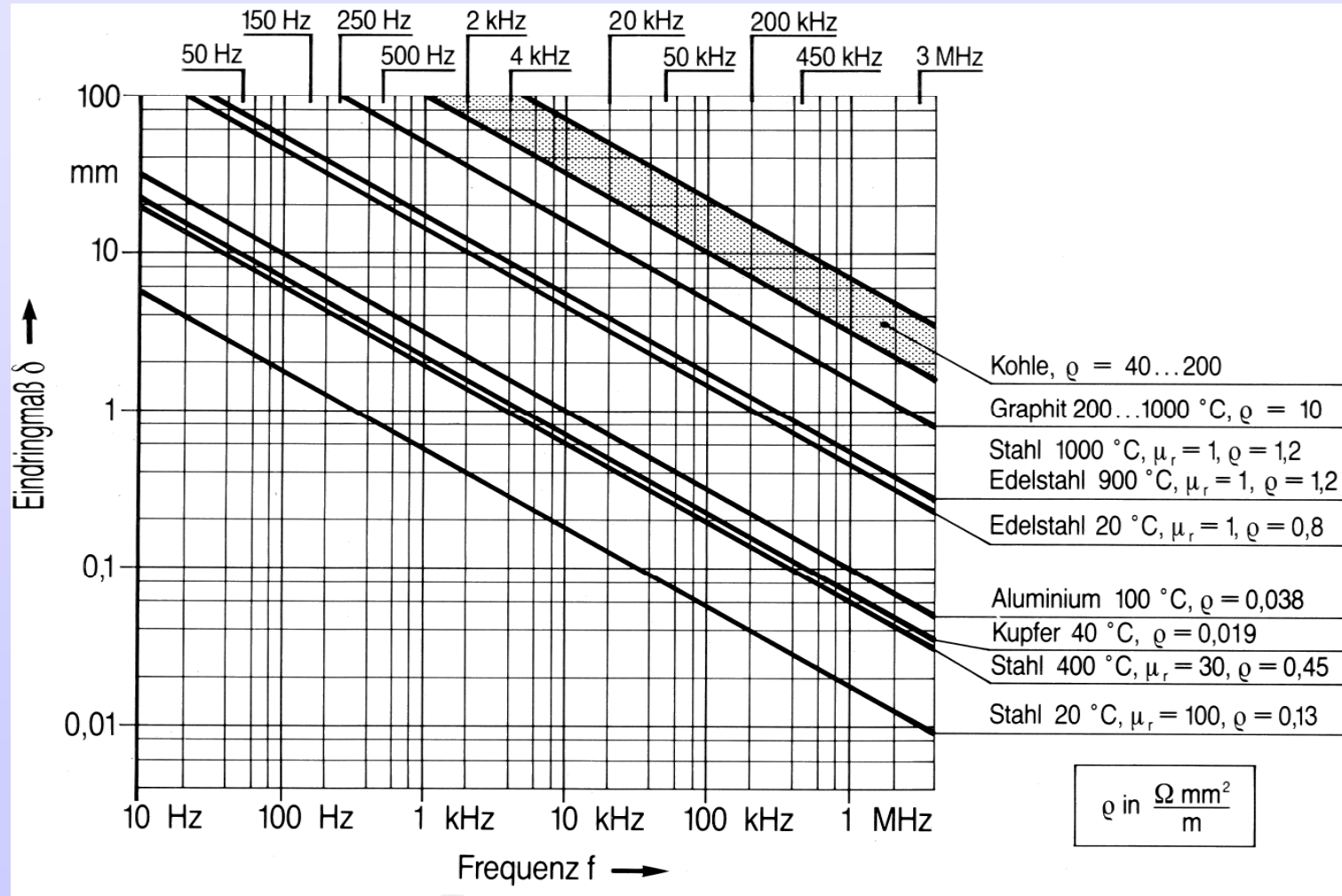
The exponential distribution of current and magnetic field is exactly valid only for **plane** surfaces (approximately valid for cylinders for  $d/\delta > 4$ )

Source: RWE-Information Induction Heating

# Electrical and thermal properties of steel (C 45)



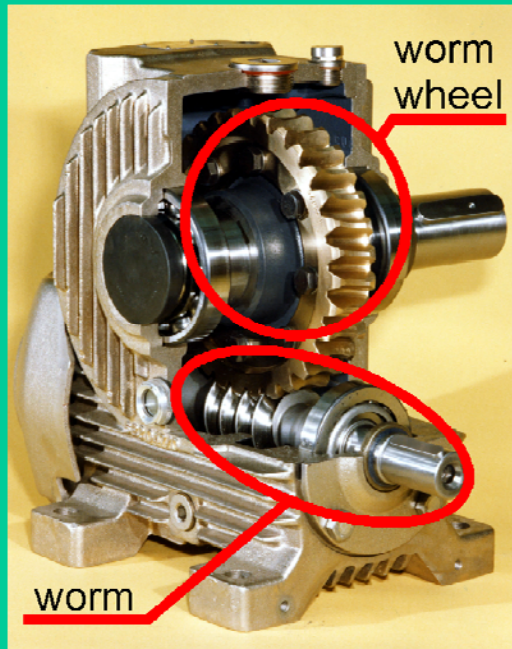
# Electromagnetic penetration depth dependent on frequency



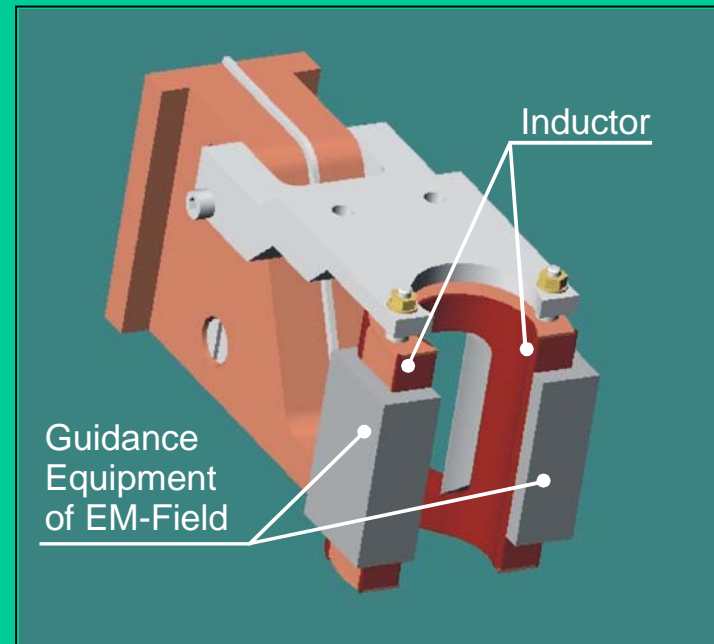
Source: RWE-Information

# Surface hardening of worm gears with dual frequency

## Worm-Gear



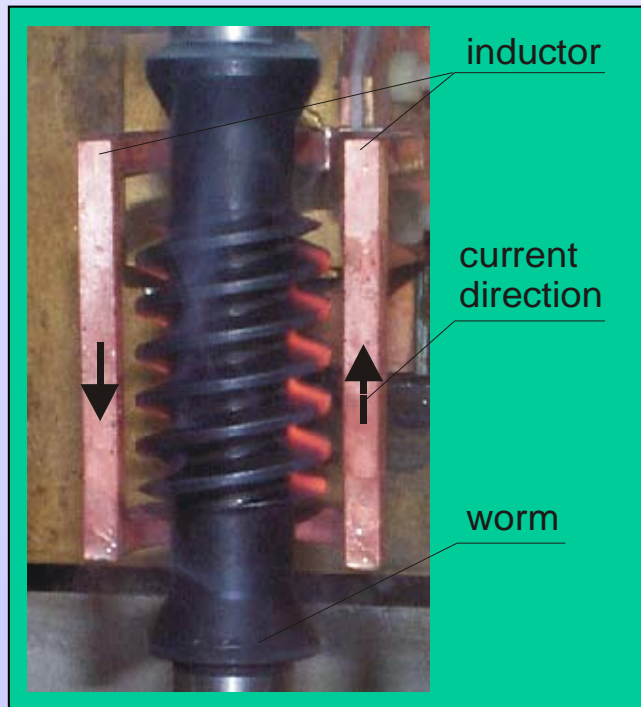
## Line-Inductor



- Aim: temperature-distribution close to the contour
  - ➔ uniform hardening-profile at the surface region

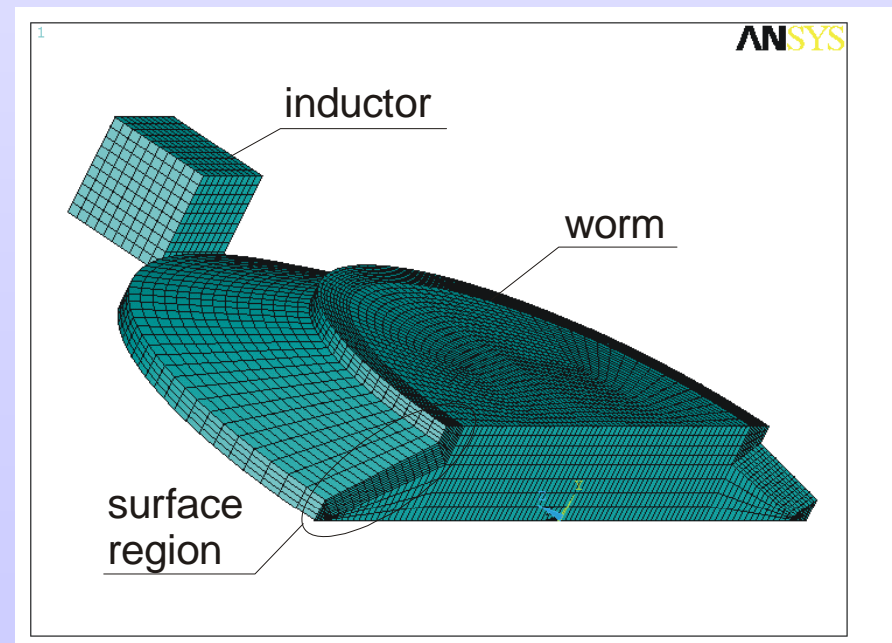
## Simulation model

- Boundary Conditions:
- heating-time: 1 s
  - maximum temperature: 950 °C
  - rotating worm



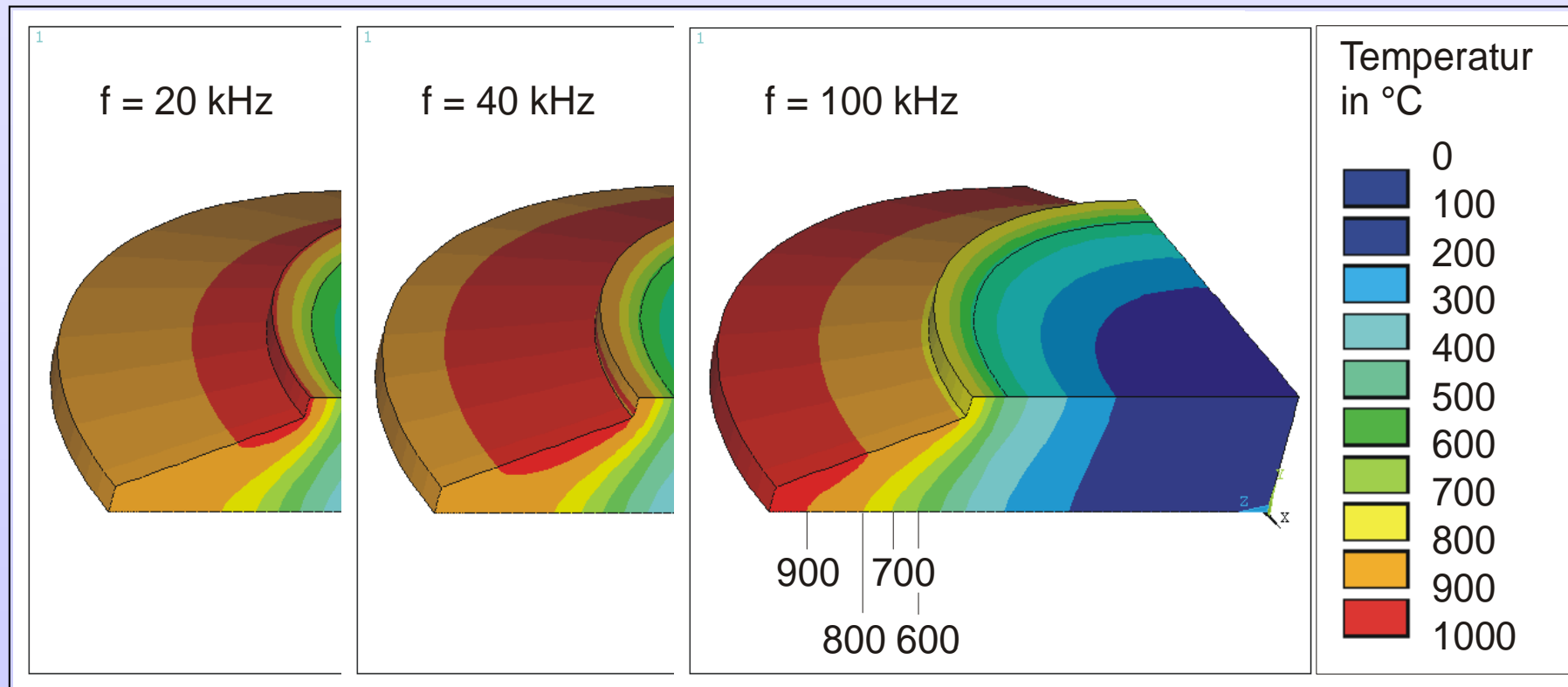
Worm with inductor

- Symmetry Conditions:
- long inductor
  - 180° in circular direction
  - gradient angle was not taken into account



Net of the simulation model

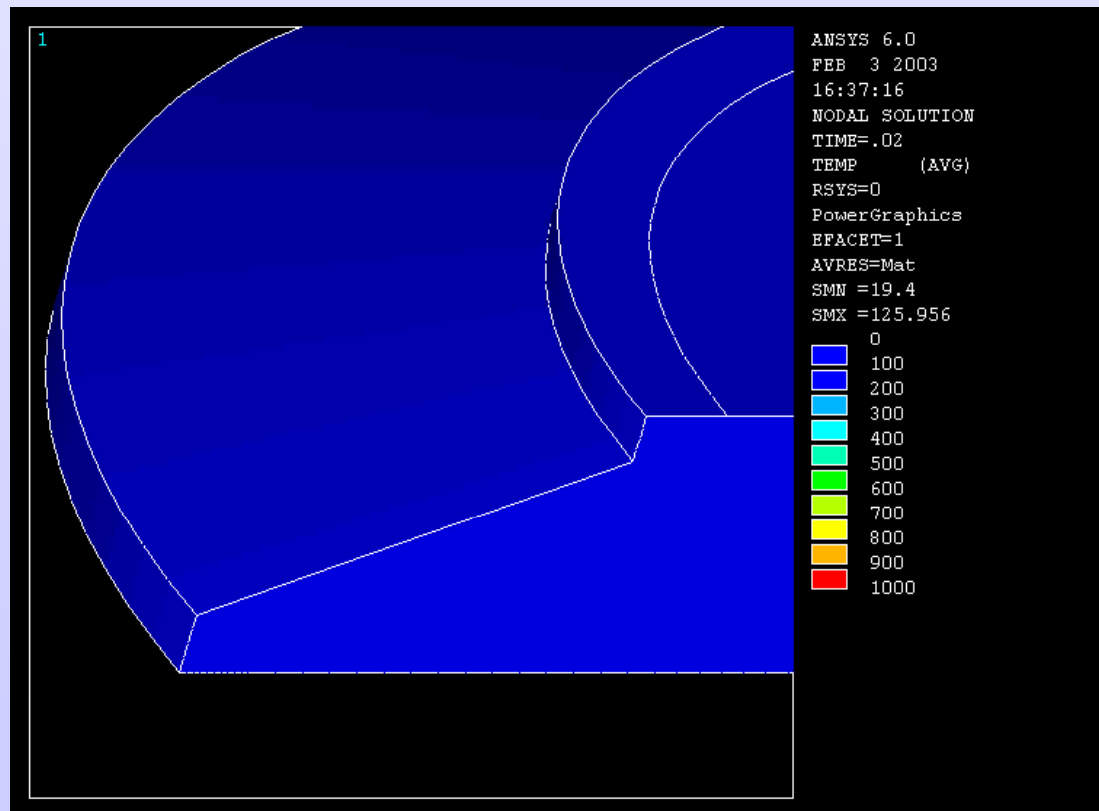
## Induction surface hardening of worm gear with single frequency



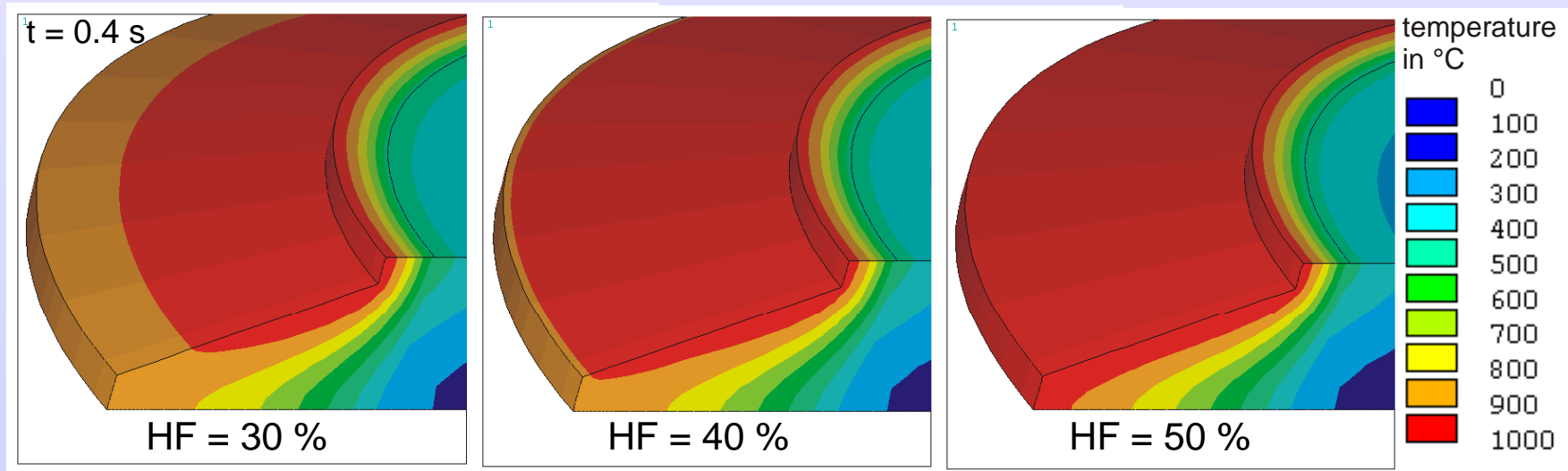
➤ No optimal solution for hardening of warm gears by single frequency

# Transient induction heating process using dual frequency (15 kHz + 300 kHz)

50% MF  
50% HF



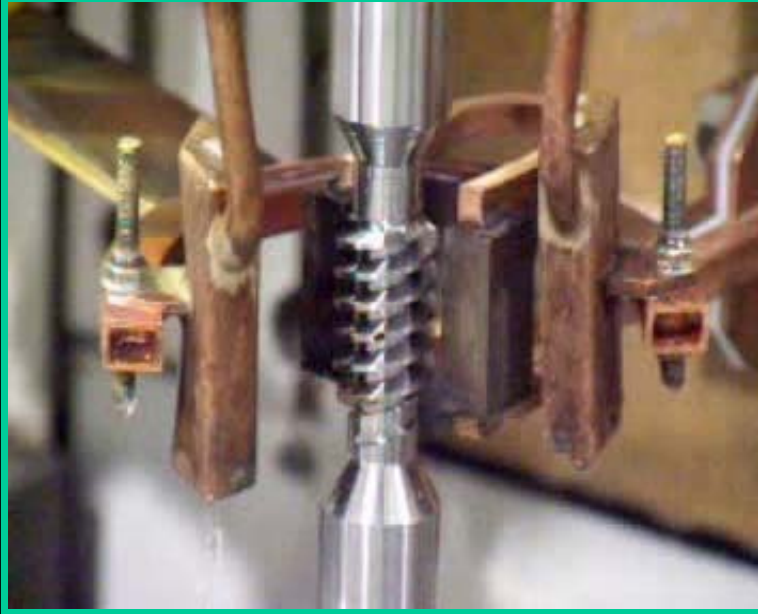
## Induction surface hardening of worm gear with dual frequency technology



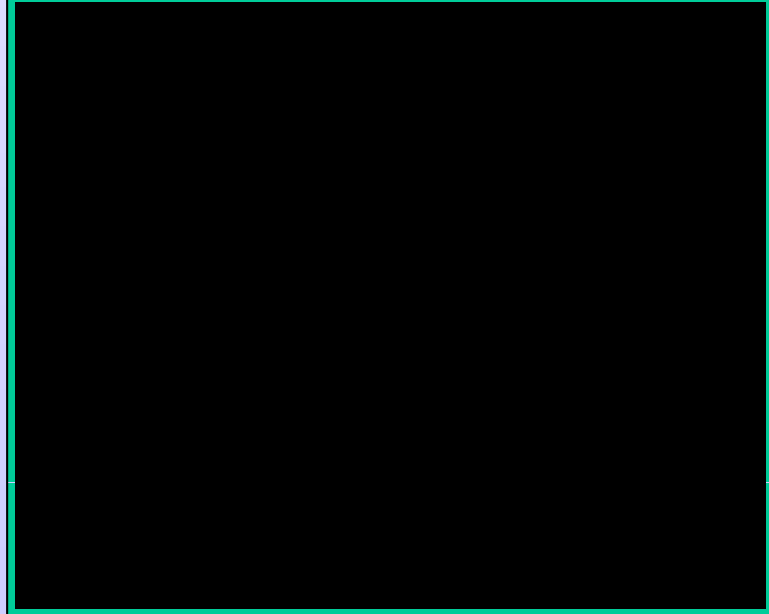
- Heating-area can be adjusted via power-ratio of MF/HF
- Getting a heating-profile close to the contour of the worm is possible
- This heating-profile enables reaching the desired hardening-profile
- Short heating time necessary to reduce the influence of heat conduction

## Experimental hardening

- 75 kW generator  
(75 kW MF, 75 kW HF)
- Heating time 1,3 s



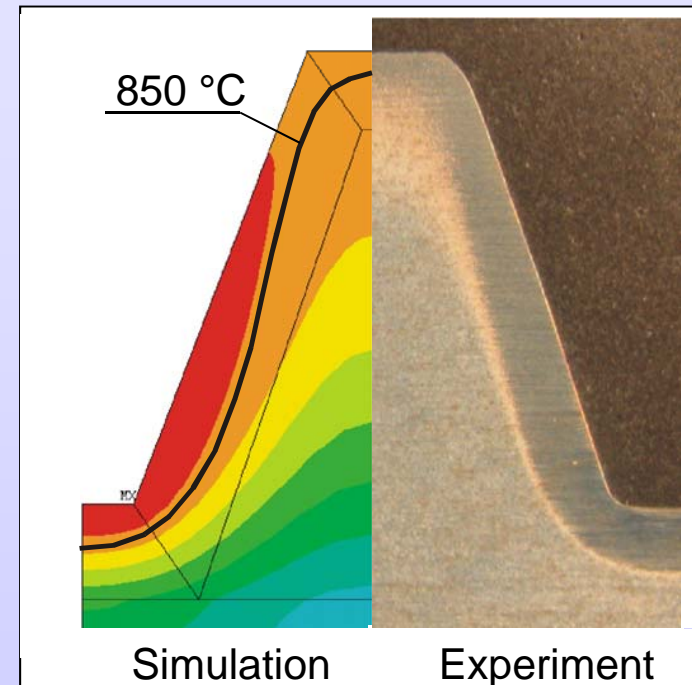
- 600 kW generator  
(400 kW MF, 200 kW HF)
- Heating time 0,35 s



# Comparison of temperature and hardness distribution

## Simulation- und hardening data

- ➔ Double frequency heating
- ➔ Total power 600 kW
- ➔ Pre heating:
  - Heating time: 0,5 s
  - HF-power: 10 %
  - MF-power: 0 %
- ➔ Heating:
  - Heating time: 0,3 s
  - HF-power: 30 %
  - MF-power: 70 %



## Conclusion

- ➔ **Good agreement** between simulated temperature und final hardness profile
- ➔ **The final hardening profile** can be excellently predicted by numerical simulation of the temperature distribution only

## Simulation of complex 3D temperature fields in systems for crystal growing of photovoltaic cells

- EFG process
- String ribbon growing process

## Edge-defined Film-fed Growth (EFG)

A silicon tube is pulled directly from the silicon melt.

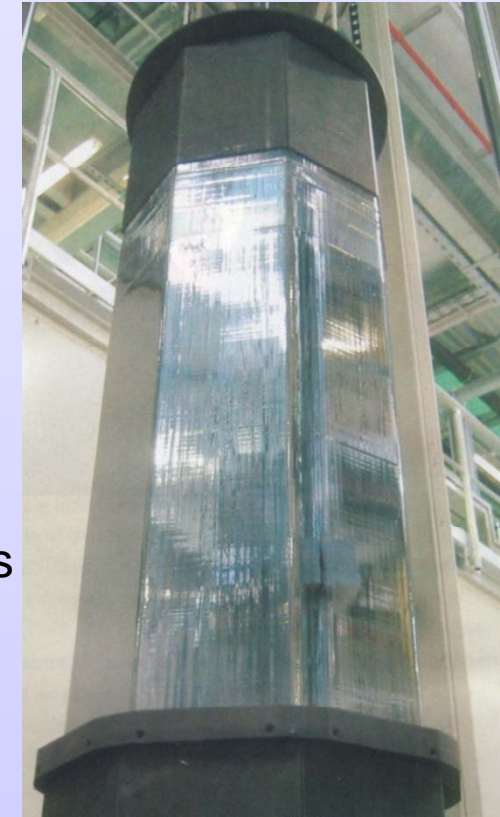
### Facts

- + 6 to 7-meter-long hollow silicon tubes
- + wall thickness of 330  $\mu\text{m}$  with the final thickness of the cells
- + a laser cutting process results into 125 mm x 125 mm wafers



### Performance of process and wafers

- + fast throughput (with feed of 20 mm/min)
- + reliable production process
- + EFG process allows to reduce the demand of silicon due to less material losses (no sewing losses)
- + high wafer quality in material grade and strength

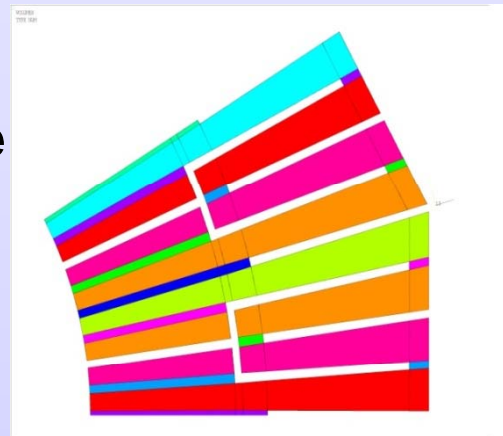


## New EFG system

larger diameter, tube with 12 sides (dodecagon)

## Advantages due to resistance heating

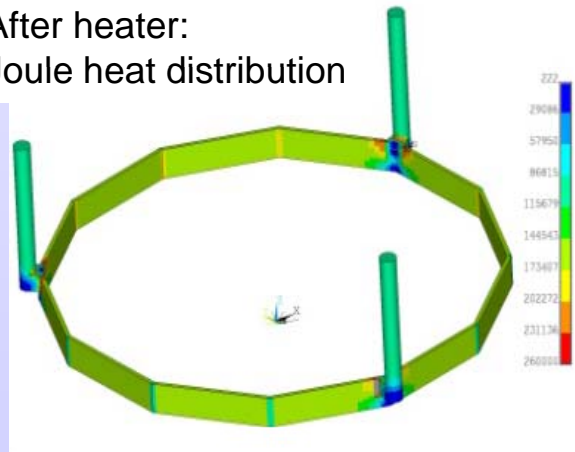
- ✚ individual adjustable 12-zoned resistance main heater
- ✚ no electromagnetic coupled system like the inductive heated melting furnace
  - ⇒ e.g. no influence of the difference of phase on the temperature distribution
- ✚ 12 sided silicon tube increases significantly the yield per pull



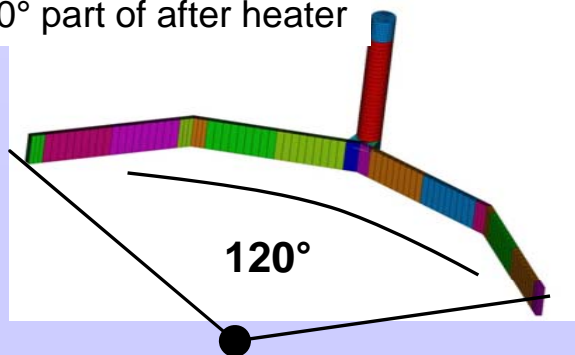
## Electromagnetic model

- + different symmetries of main and after heater
  - ⇒ two separate models: coupled 30° model for main heater and 120° thermal model for after heater
  - ⇒ import of heat sources into the 120° thermal model

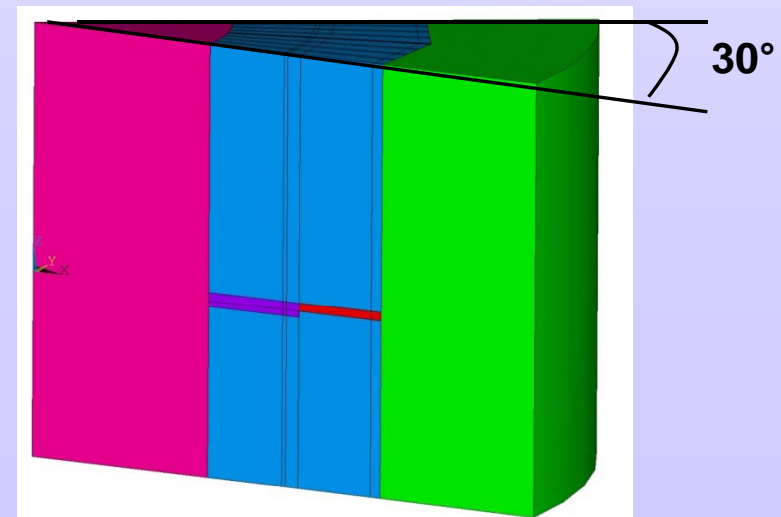
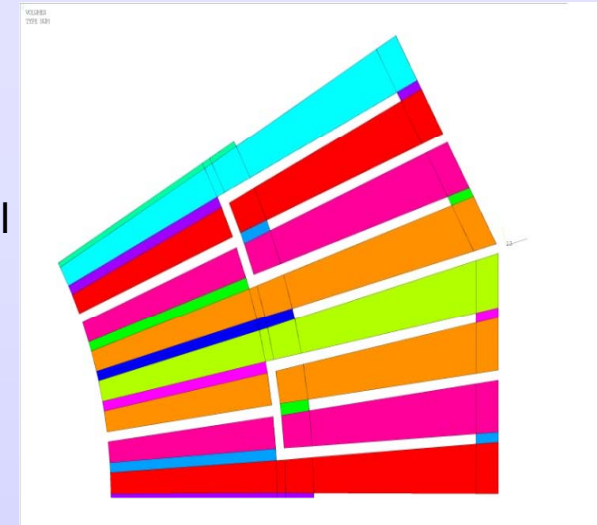
After heater:  
Joule heat distribution



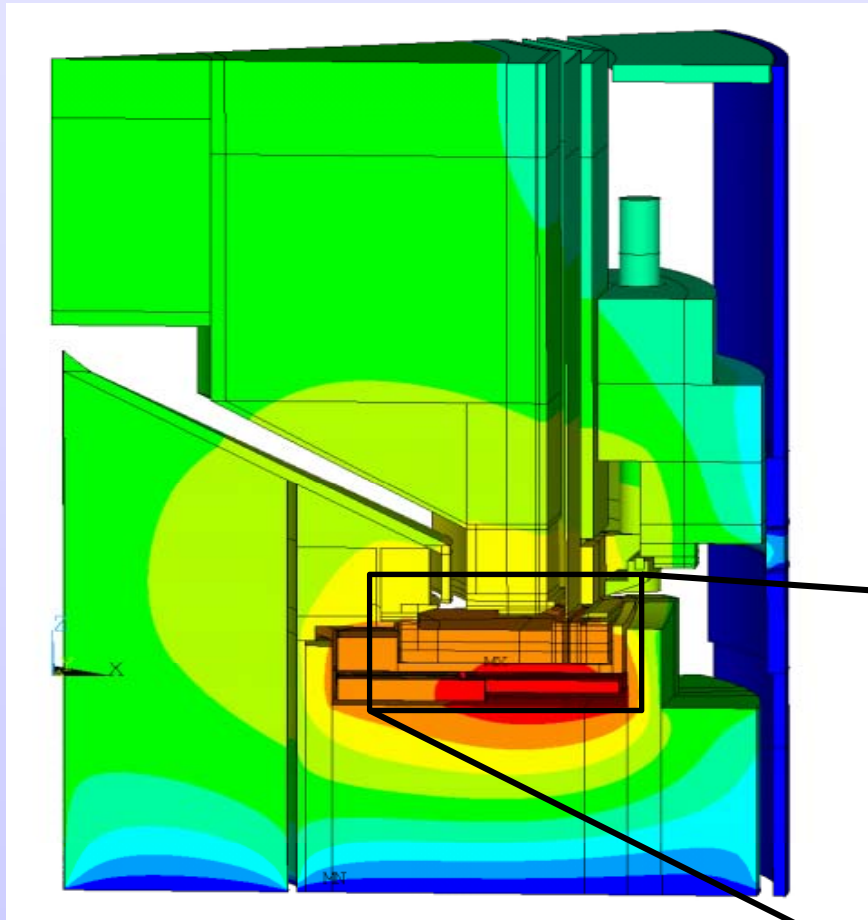
120° part of after heater



Main heater

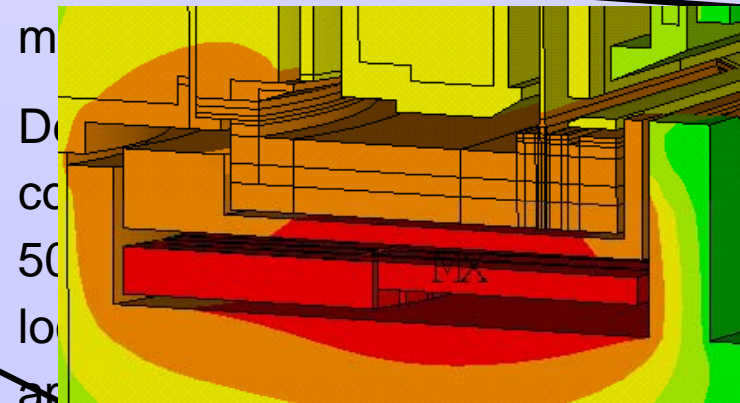
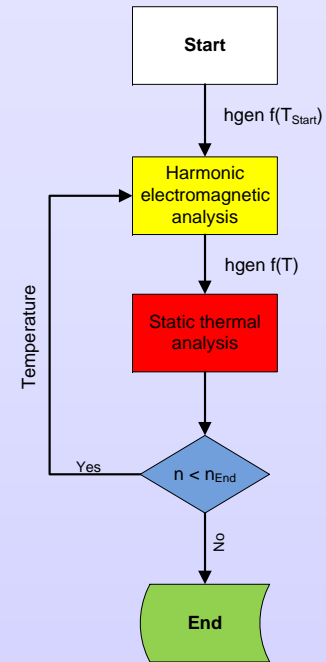


# Temperature distribution calculated by coupled 30° model



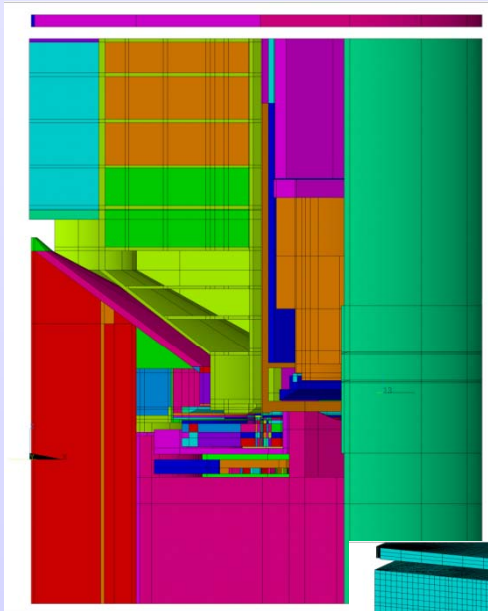
Result of temperature distribution  
(after 3 iteration loops)

- ✦ Temperature dependent thermal analysis of joule heat generation in main and after heater
- ✦ 30°-geometry for faster calculation (approx. 20% in size compared to 120°-



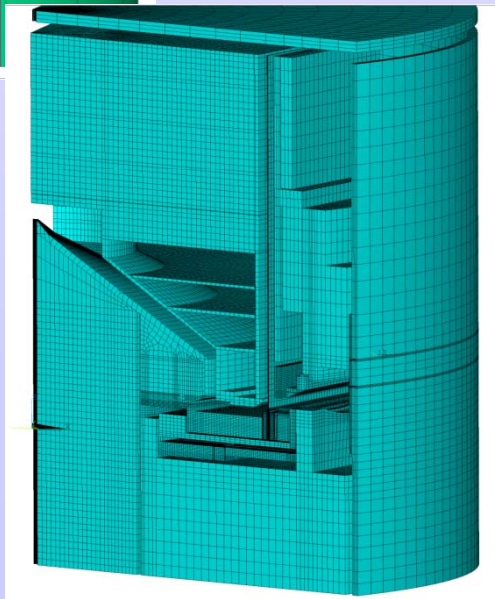
Cut out at larger scale

# Temperature distribution calculated by thermal 120° model

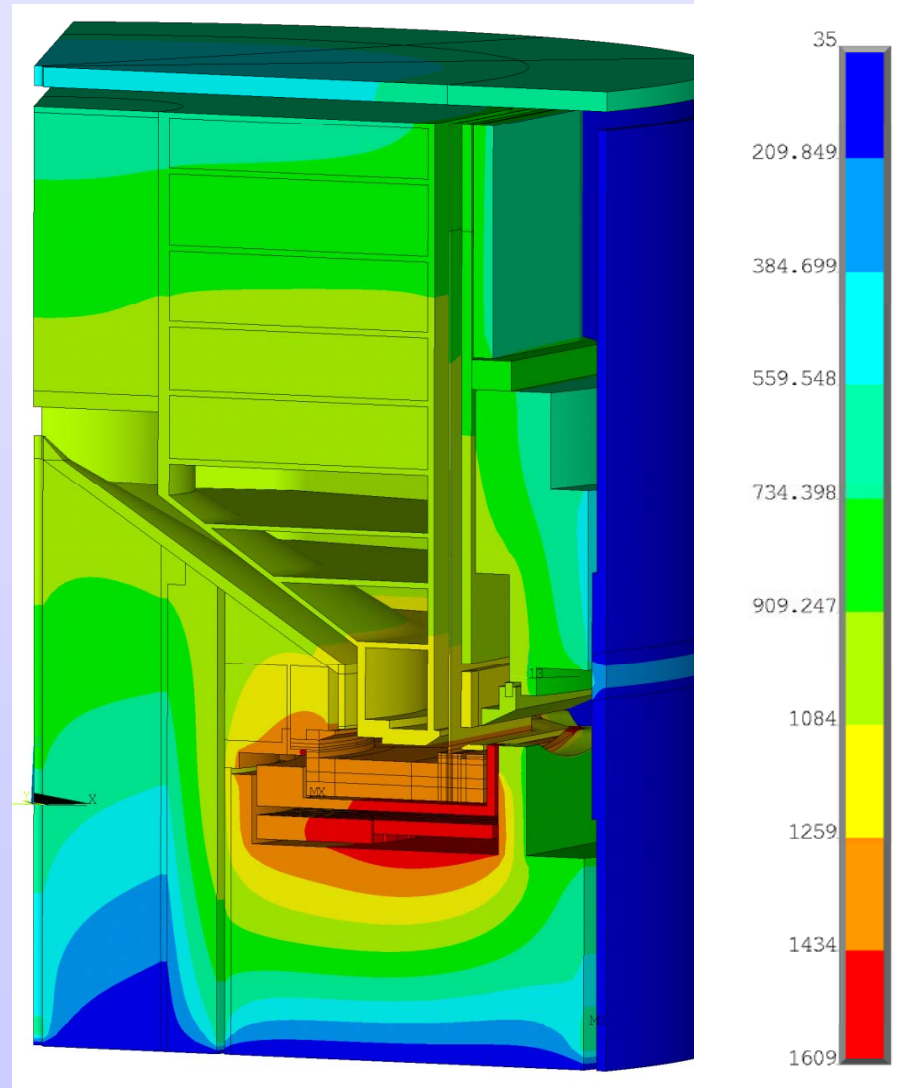


Temperature distribution

Zones of numerical model



Mesh



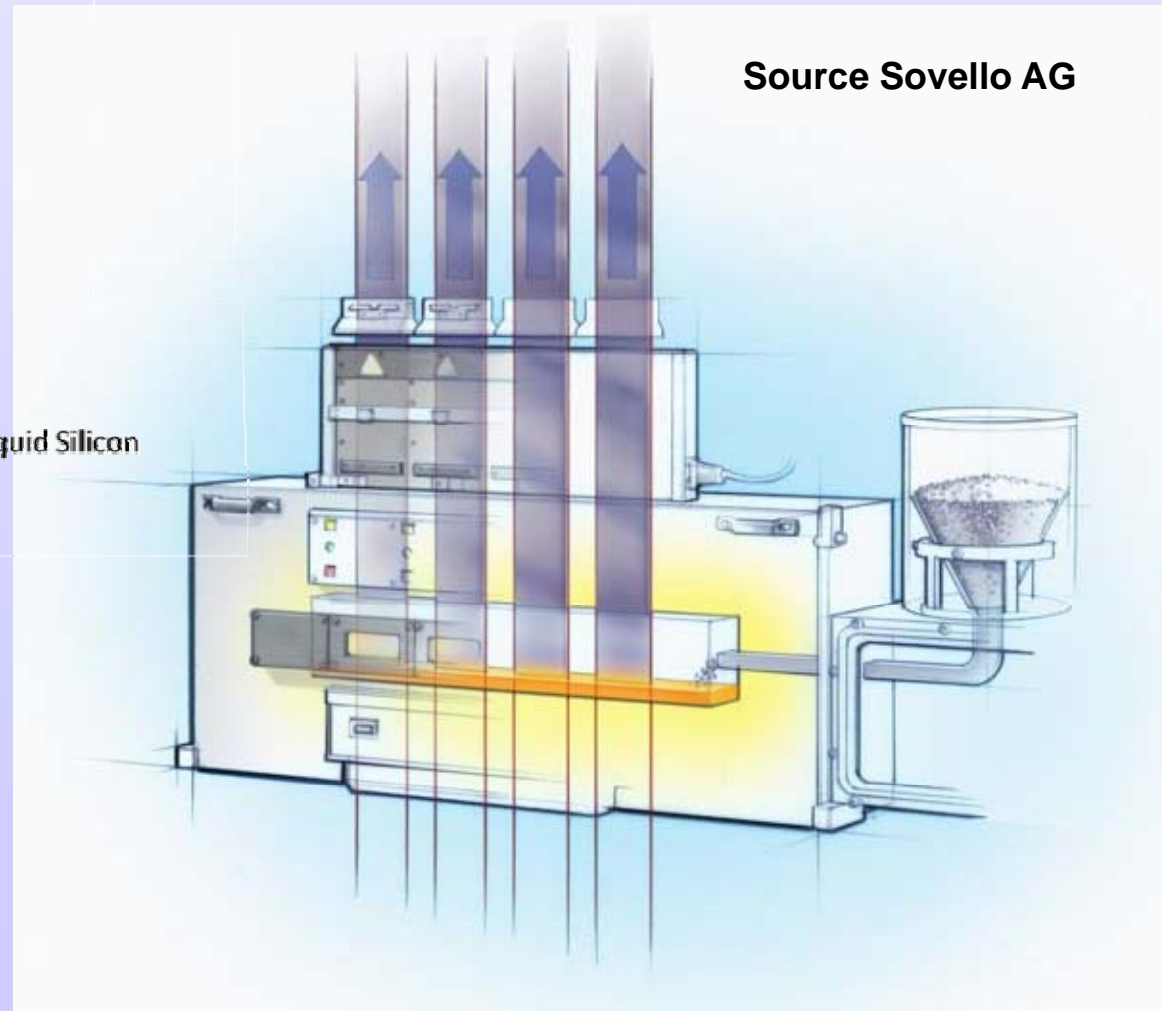
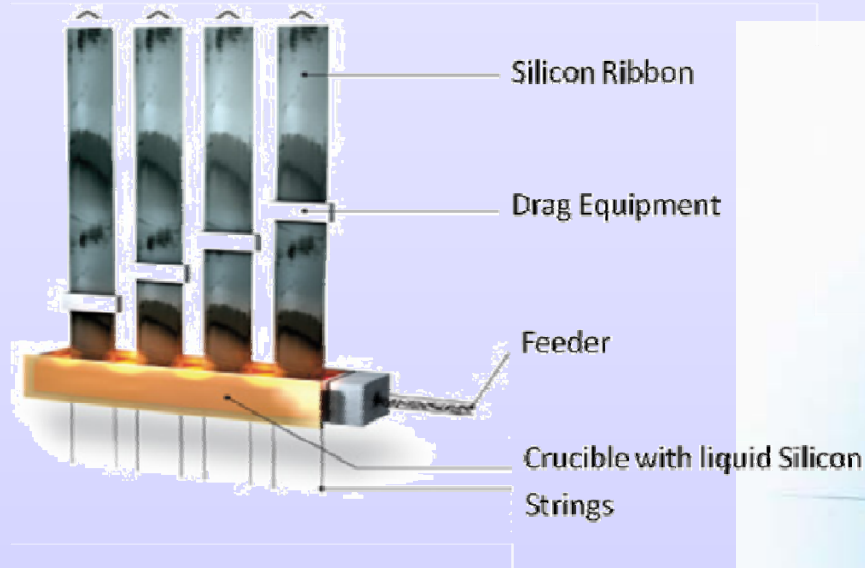
## Coupled 30° model

- ✚ required harddisk space ~ 245 GByte (about 220 GByte viewfactor-matrix)
- ✚ calculation time: approx. 75 h (max. 2 cores\*, intel Core 2 Quad 9450, 8 GB-RAM) 3 iterations loops
- ✚ approx. 786.000 notes
- ✚ approx. 285.700 radiation surfaces
- ✚ RAM-usage ~ 7,9 GByte

## Thermal 120° model

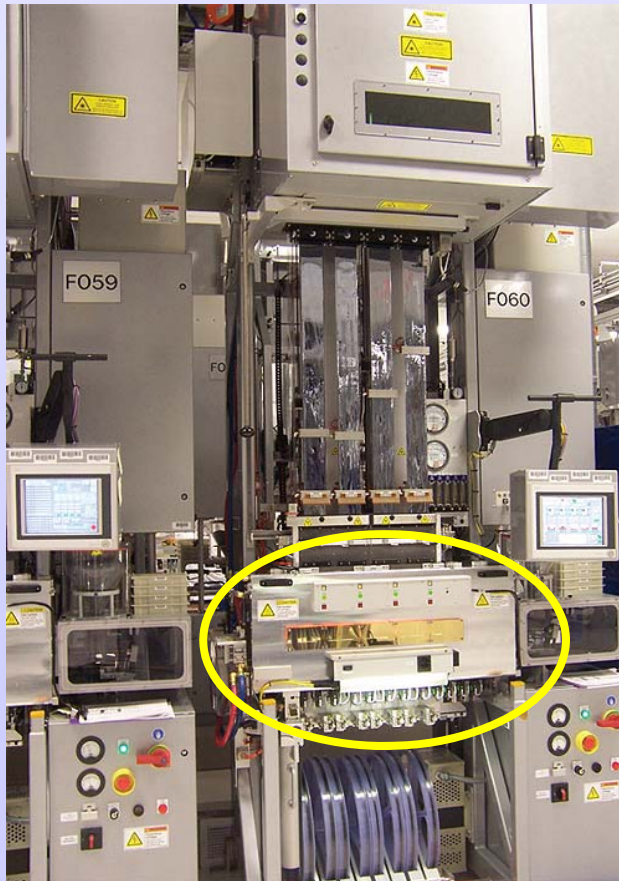
- ✚ required harddisk space ~ 1165 GByte (about 1100 GByte viewfactor-matrix)
- ✚ calculation time: approx. 150 h (max. 2 cores\*, intel Core 2 Quad 9450, 8 GB-RAM) for stationary solution
- ✚ approx. 1.800.000 notes
- ✚ approx. 654.000 radiation surfaces
- ✚ RAM-usage ~ 11,6 GByte

\*radiation calculations are always single core calculations in Ansys

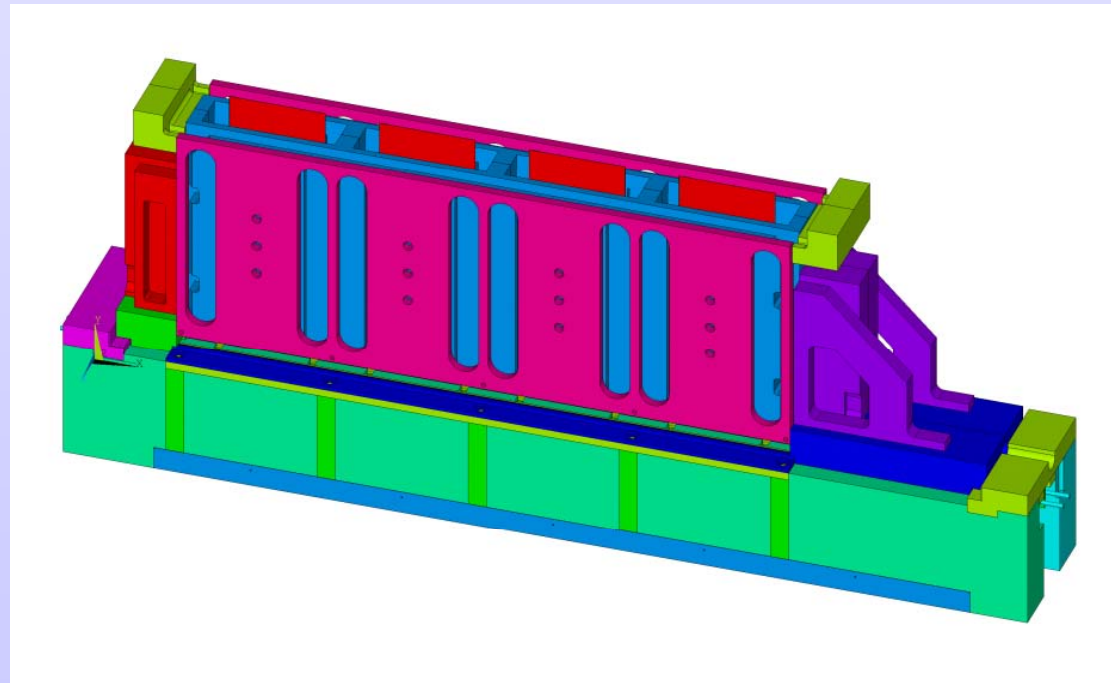


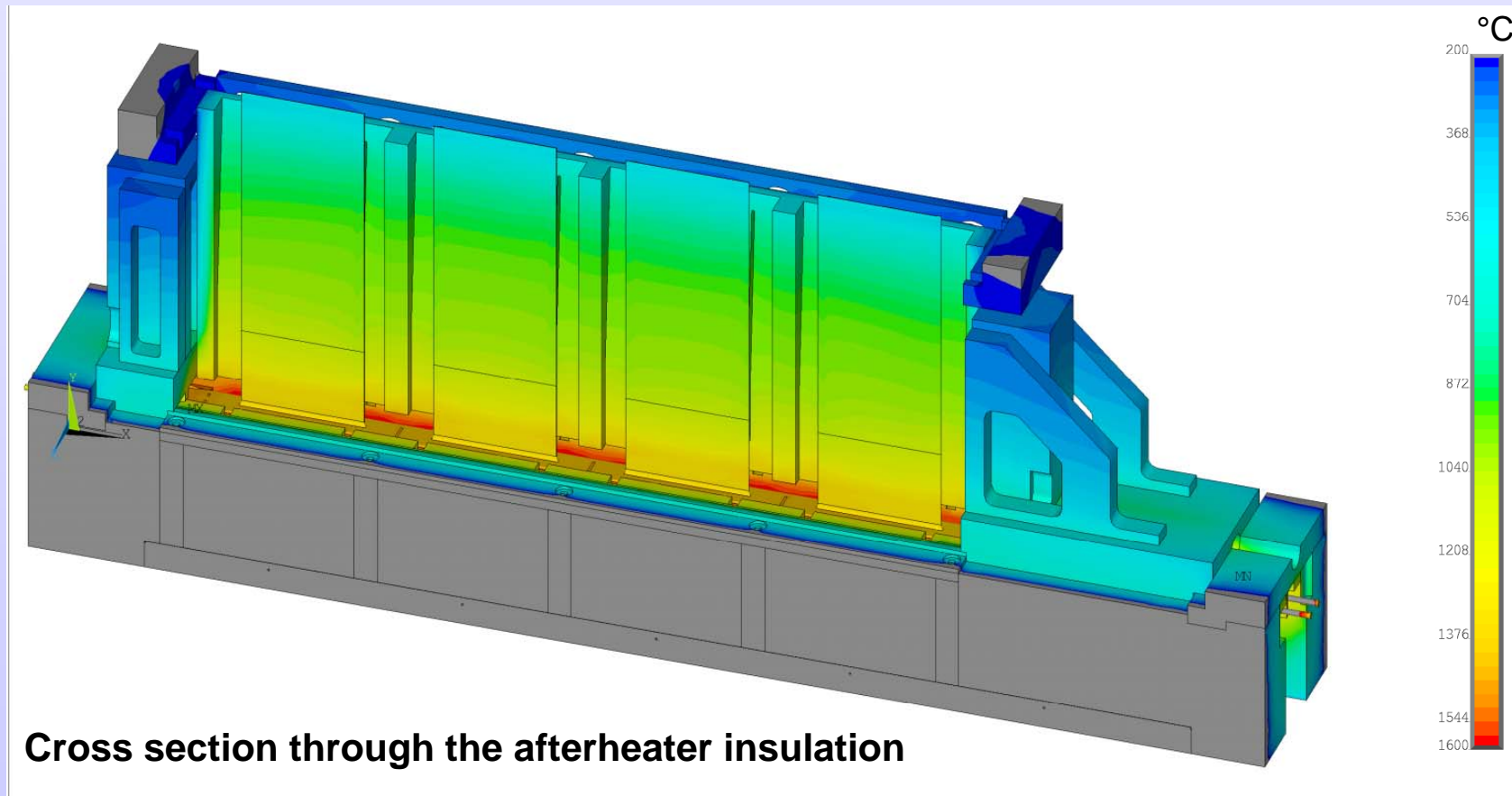
## Advantages of the process:

- + great temperature tolerance and excellent growth stability
- + no need of wafer sawing
- + low power consumption
- + average cell efficiency above 15%

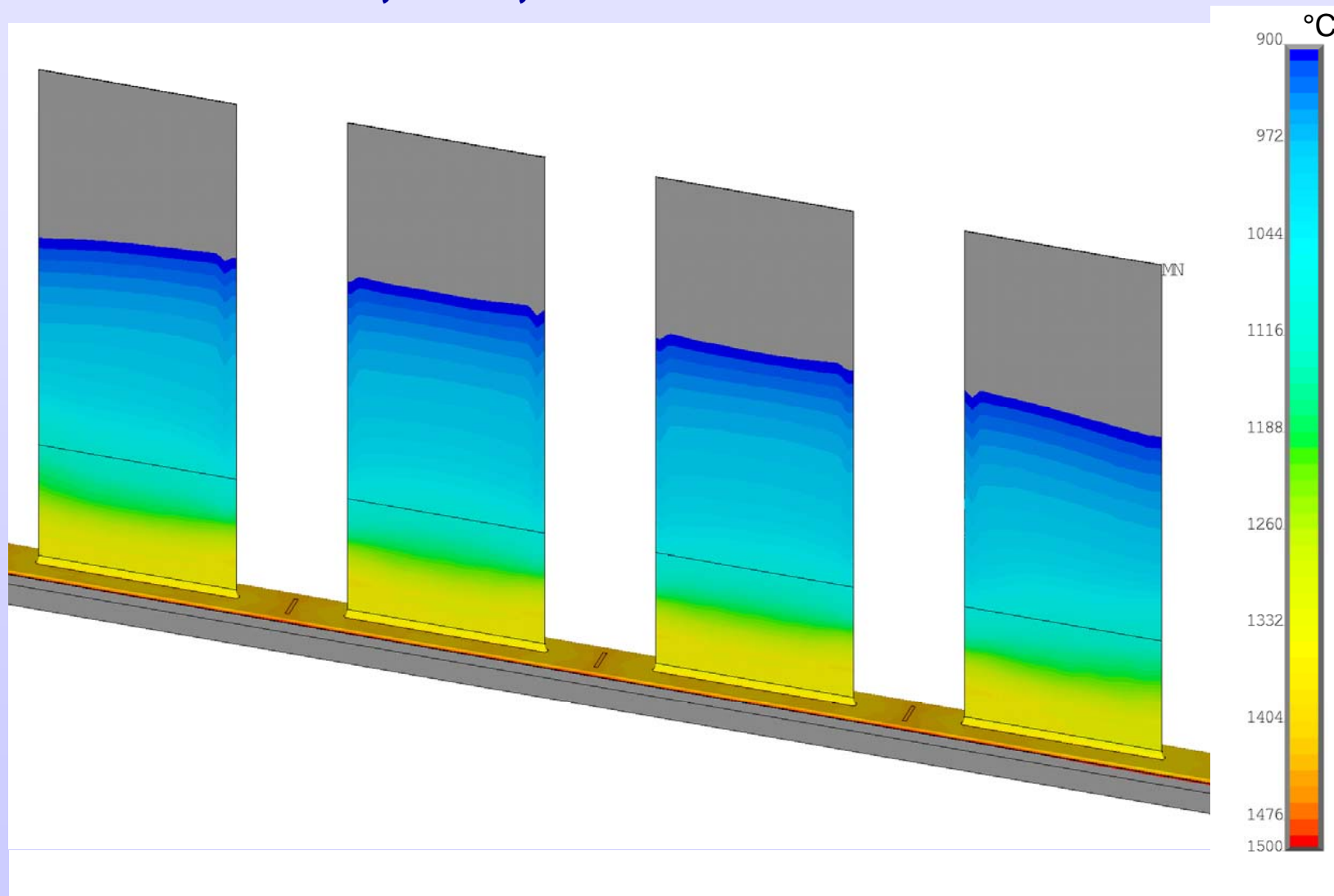


Sovello: Quad furnace in production line





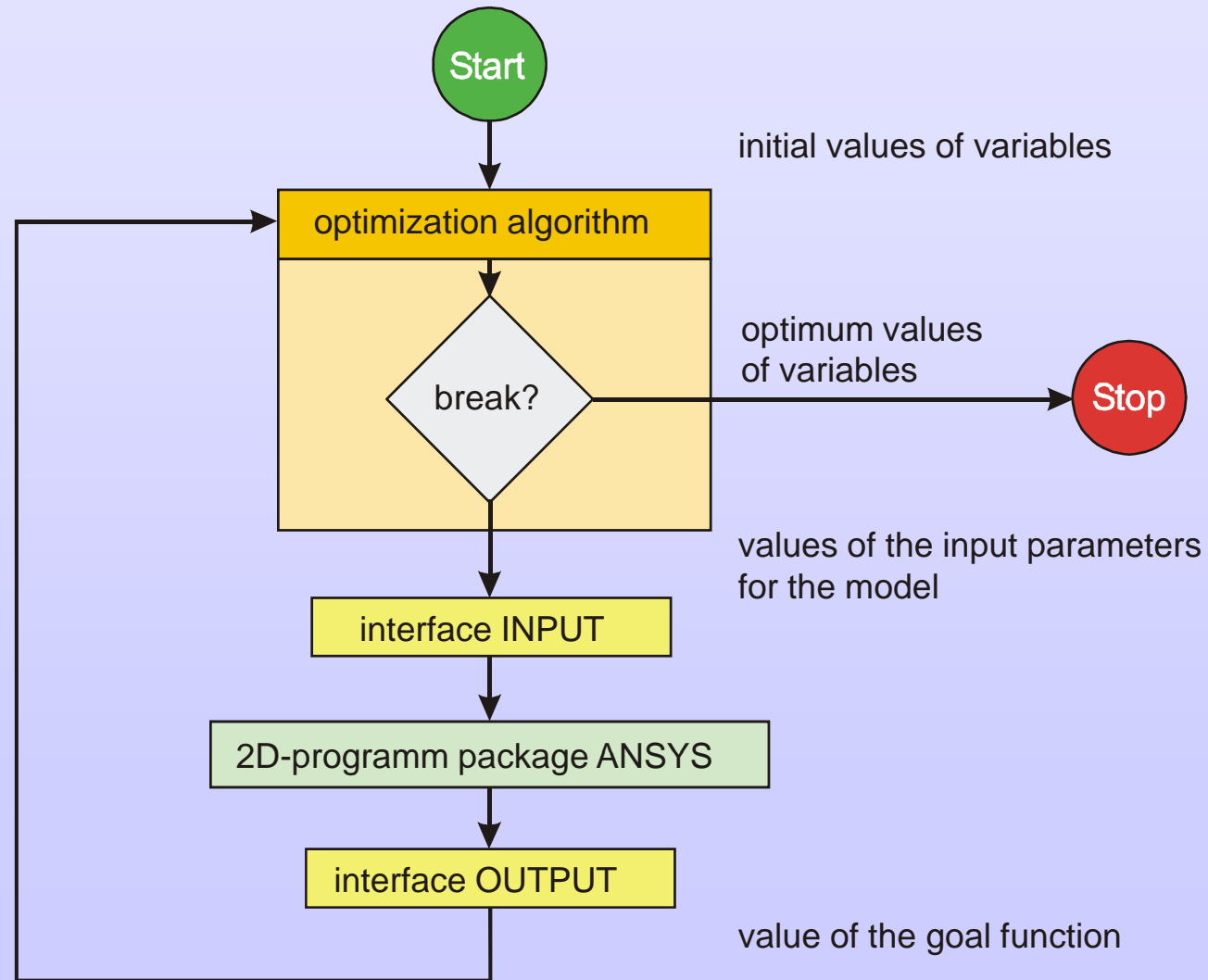
# Temperature distribution in crucible, melt, meniscus and ribbons



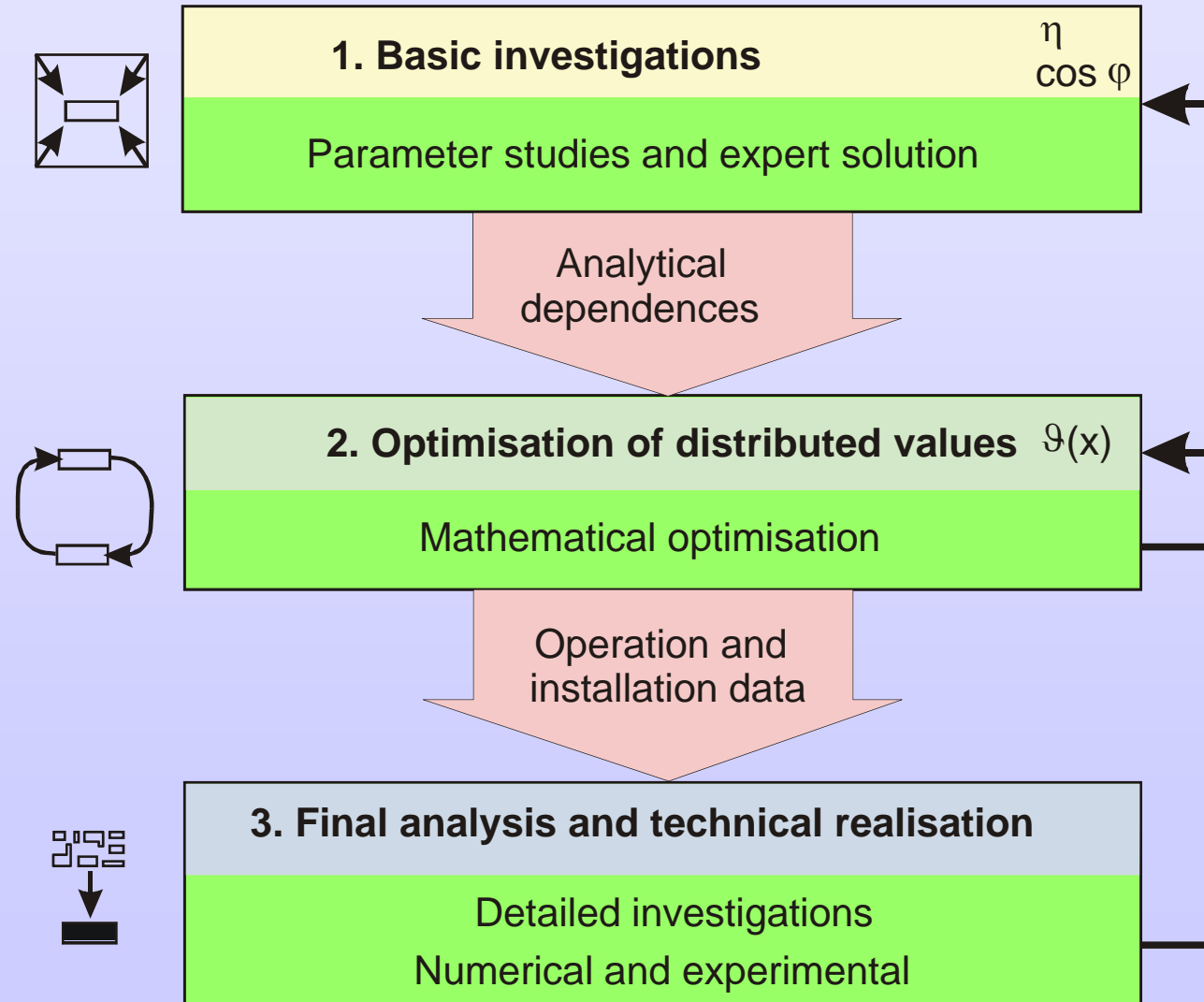
## Optimal design and process control of induction heated systems using mathematical optimization

- Tools and general aspects
- Transverse flux heating
- Planetary reactors for epitaxy processes

## 2D model combined with optimization algorithm



# Concept of optimal design



# Design of a transverse flux heater

## Requirements

### Strip

- Material: Copper + alloys
- Width: fixed: 420 mm
- Thickness: variable: 0,3 mm - 1,5 mm

### Temperature

- Heating up: from 20 °C to 300 °C
- Temp. profile: homogeneous (+-4%)

Pre heating before gas fired  
furnace of an annealing line



Improvement of productivity

## Analytical investigation

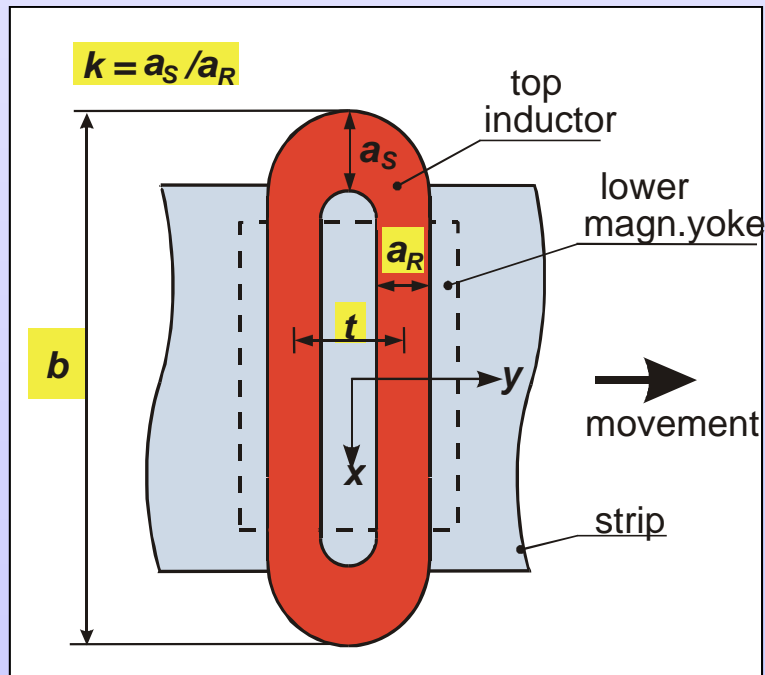
### Working areas

- Pol pitch  $t$ :  
80 mm to 300 mm

- Frequency  $f$   
in Hz for CuZn37:

$d$	$t = 80 \text{ mm}$	$t = 300 \text{ mm}$
0,3 mm	1870 Hz	500 Hz
0,8 mm	700 Hz	190 Hz
1,5 mm	370 Hz	100 Hz

# Design of a transverse flux heater by means of mathematical optimization



design variables	limits	results
inductor length $b$	350 mm - 600 mm	462 mm
cond. width $a_R$	32 mm - 160 mm	122 mm
coil head factor $k$	0,3 - 1,5	0,6
pol pitch $t$	80 mm - 300 mm	220 mm
(frequency $f = f_{opt}$ )	190 Hz - 700 Hz	255 Hz)

minimum of goal function:



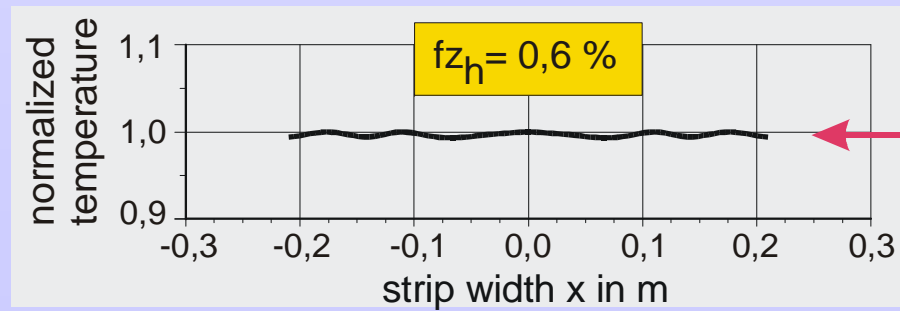
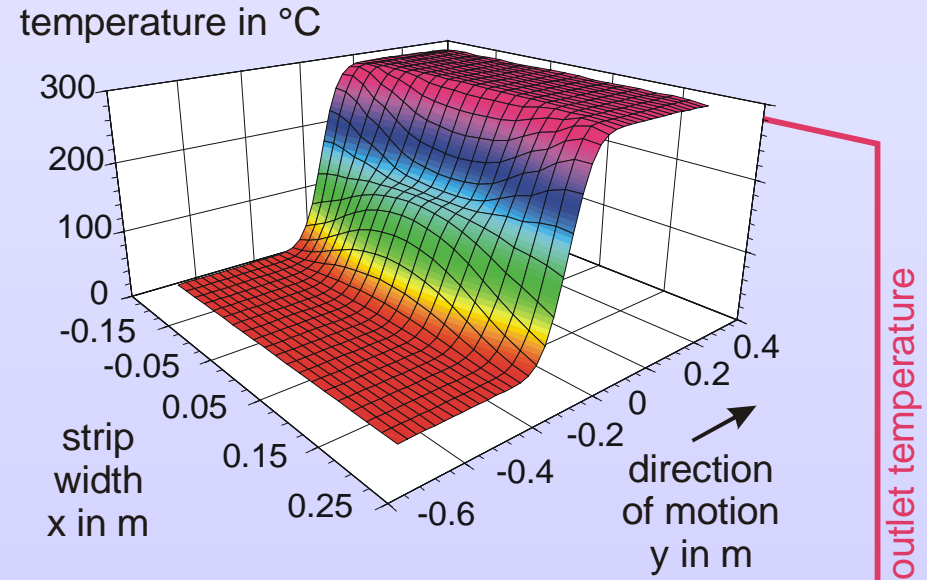
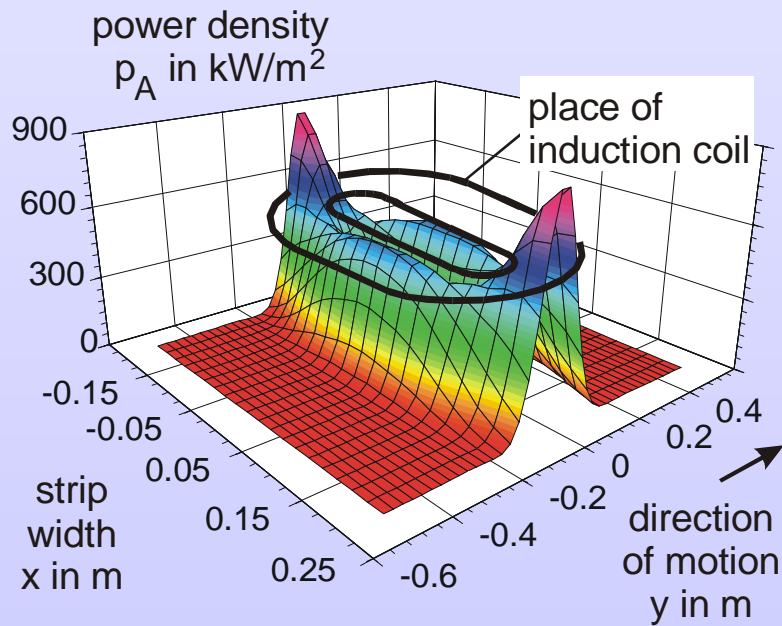
$$f_{z_h} = 0,6 \%$$

with

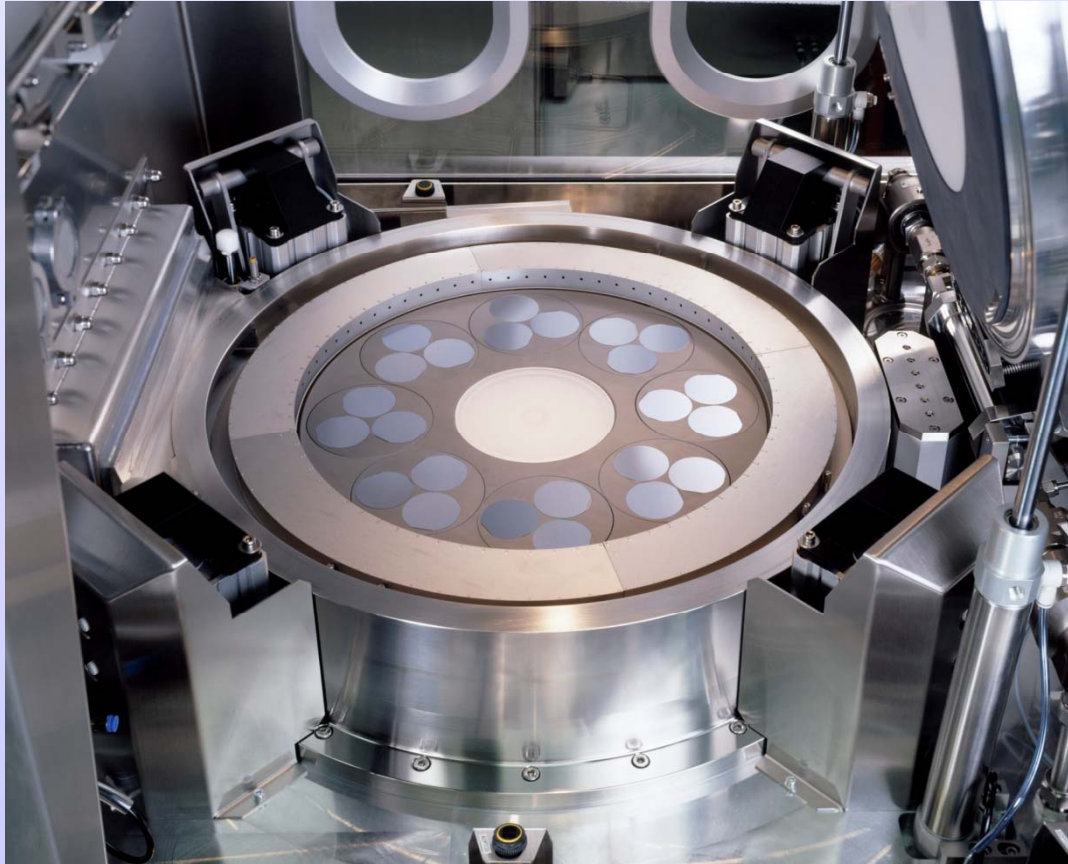
$$\eta_{el} = 94,4 \%$$

$$\cos \varphi = 0,79$$

# Results of optimization for fixed strip width



## Planetary reactors for epitaxy processes



Typical planetary reactor for epitaxy processes

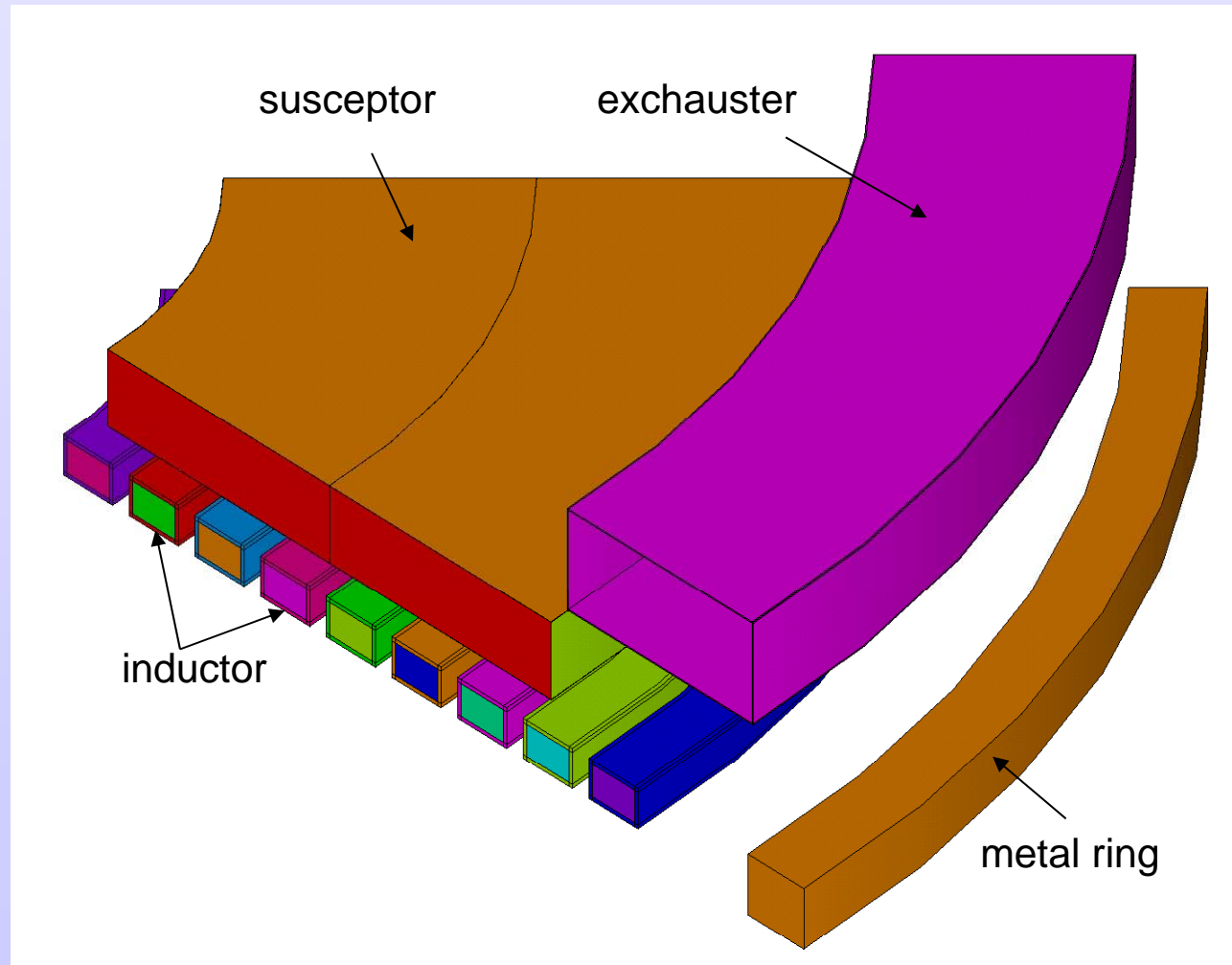
The process temperature above  $1100^{\circ}\text{C}$  is provided by induction heating of the graphite susceptor. The susceptor is covered with SiC layer because of chemically aggressive gas.

The SiC layer lifetime determines the susceptor lifetime.

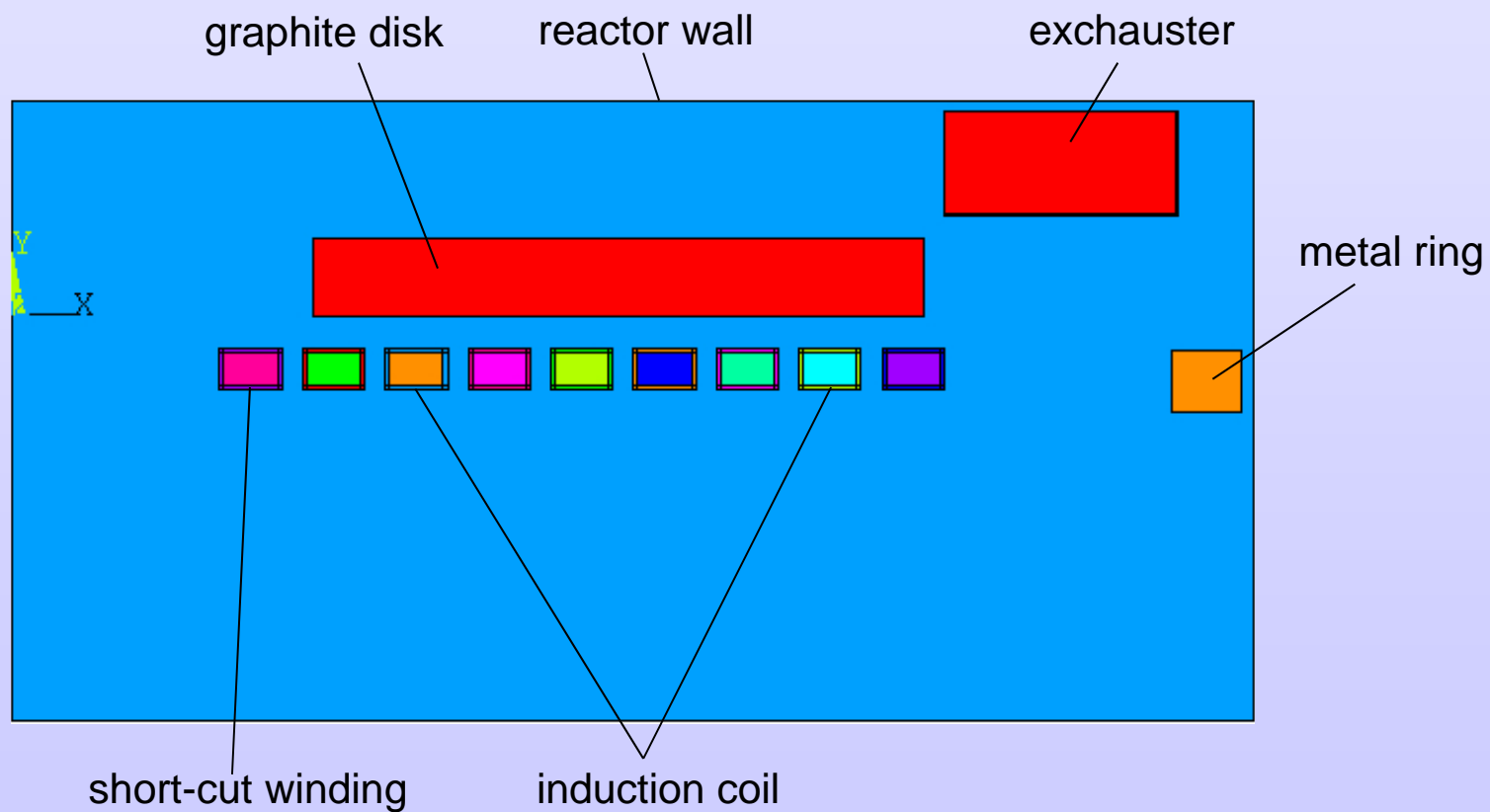
**Problem:**

Temperature gradients in the graphite create cracks in the SiC layer.

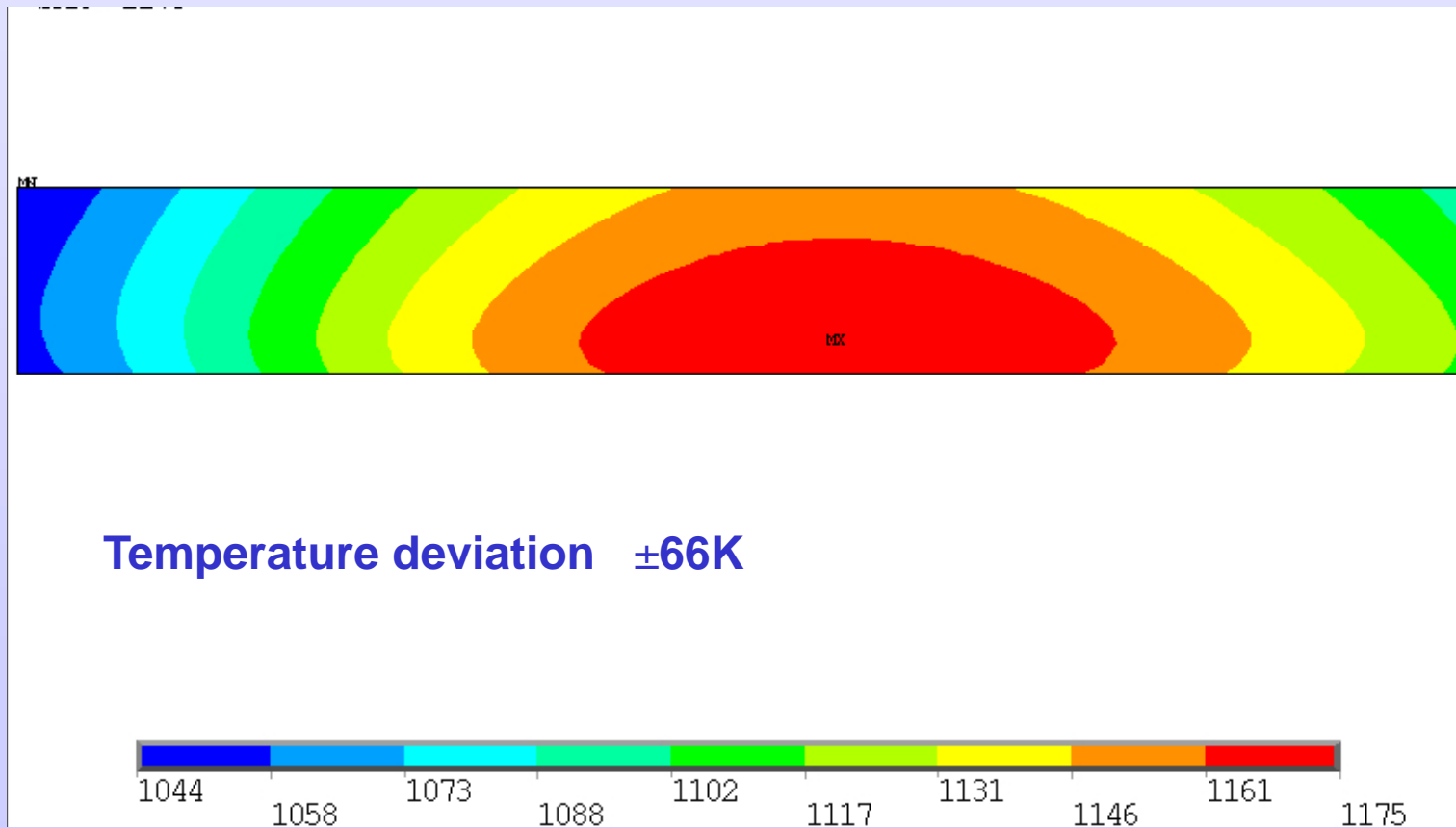
## 3D model of planetary reactor



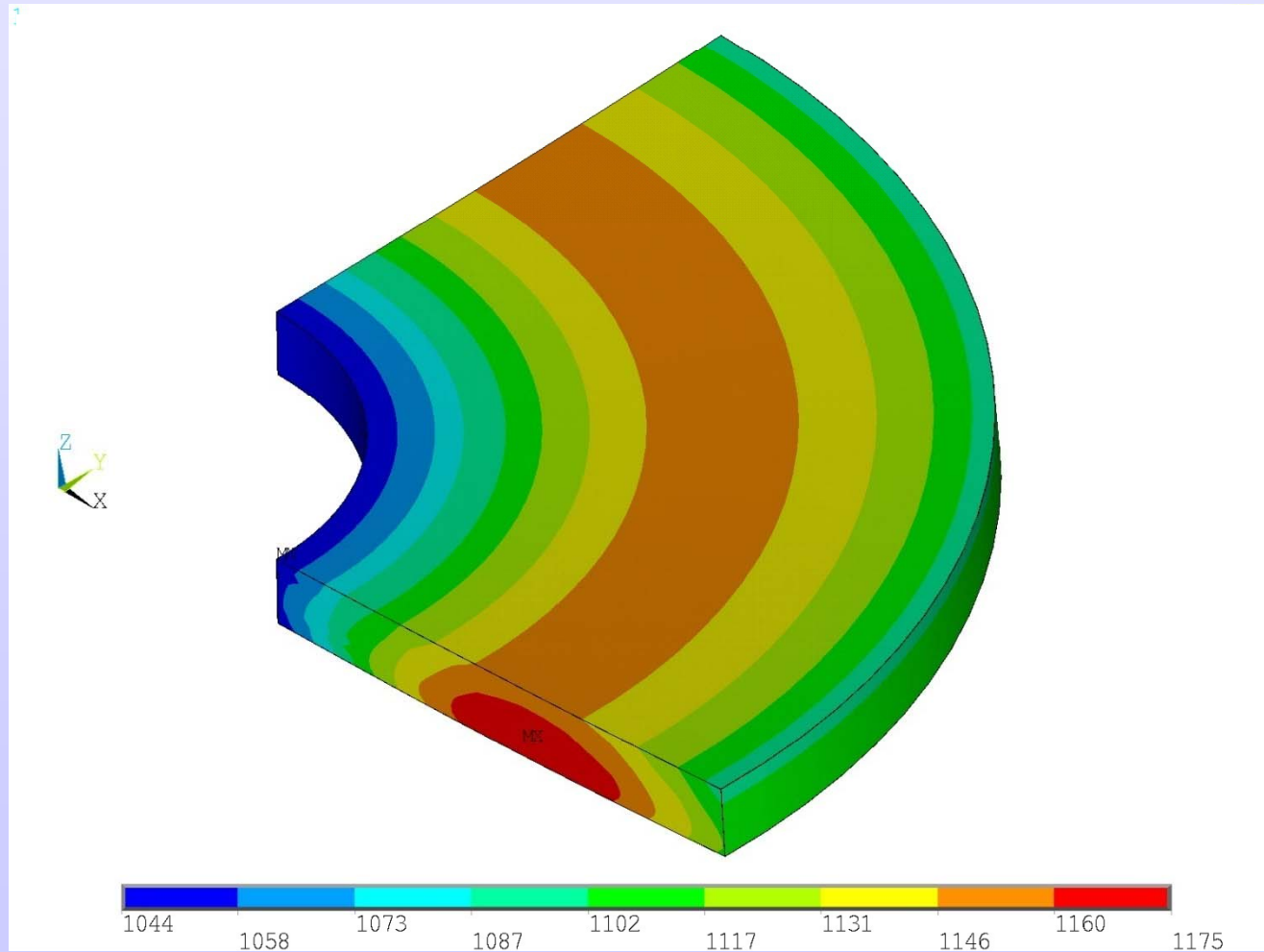
## Numerical modelling – 2D approach



## 2D temperature distribution in the susceptor for the existing system



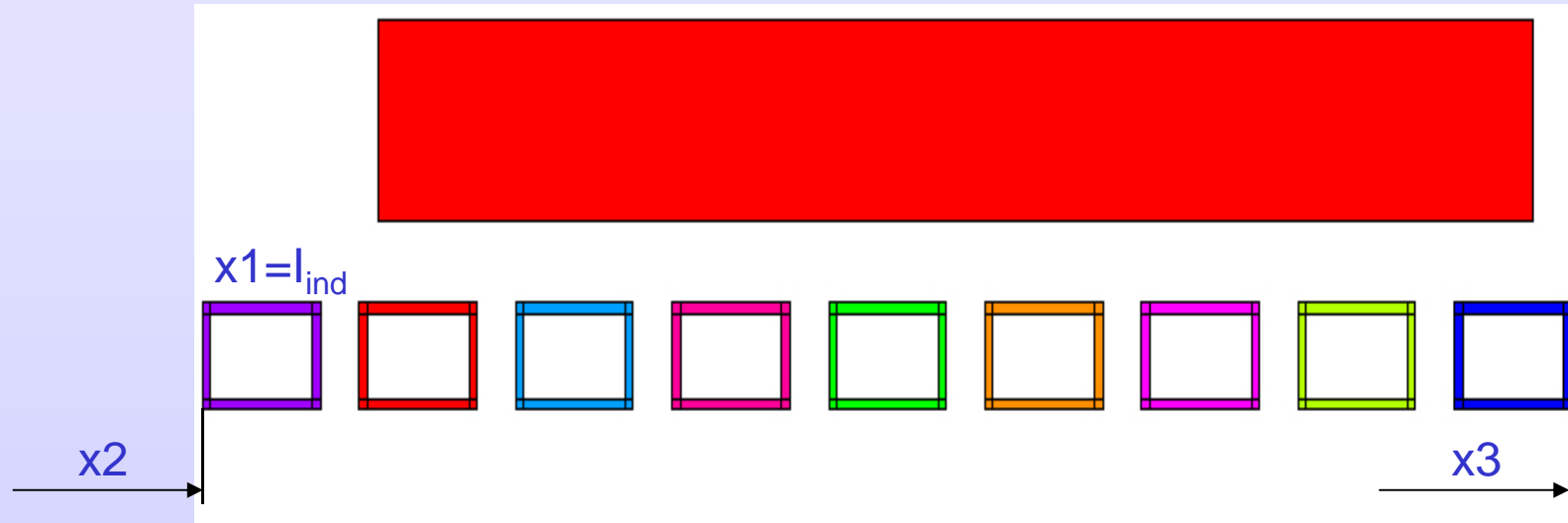
## 2D temperature distribution interpolated for 3D structural analysis



Maximum strain  
in the SiC layer  
for the temperature  
distribution is

**215 Mpa**

## Definition of optimization variables and goal function



Independent variables for optimization:

$x_1$  – current in the coil

$x_2$  – inner radius of the coil

$x_3$  – outer radius of the coil

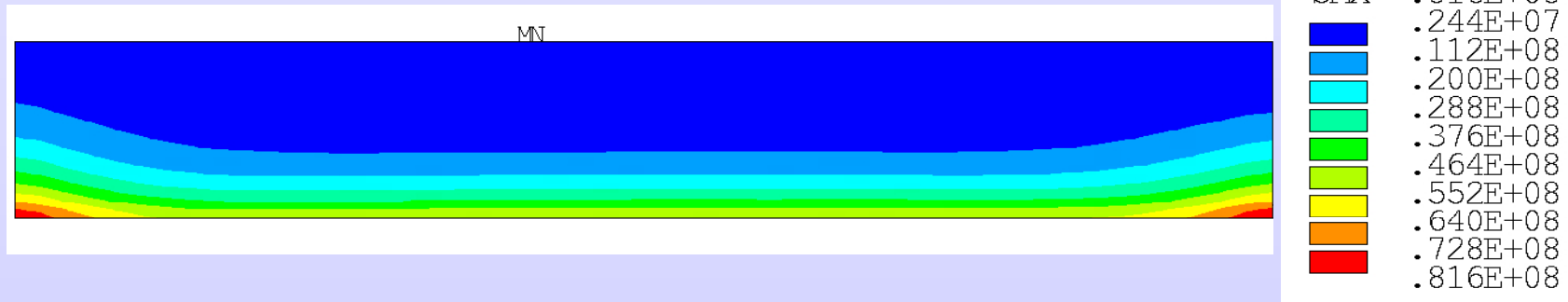
(uniform spacing between the coil windings)

Goal function to be minimized:

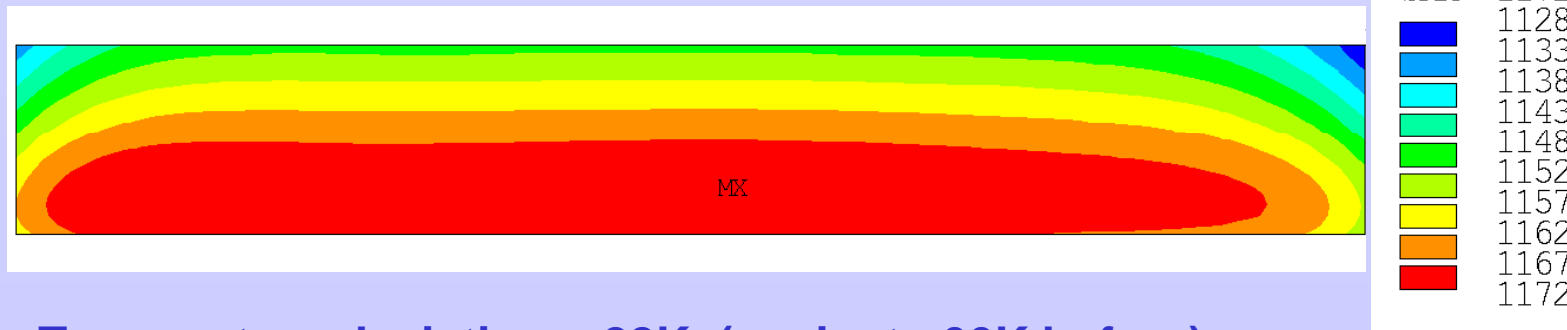
$$F = \max\{\text{abs}[T(x,y) - 1150]\}$$

# Joule heat distribution and temperature field in the susceptor for the optimized system

Joule heat

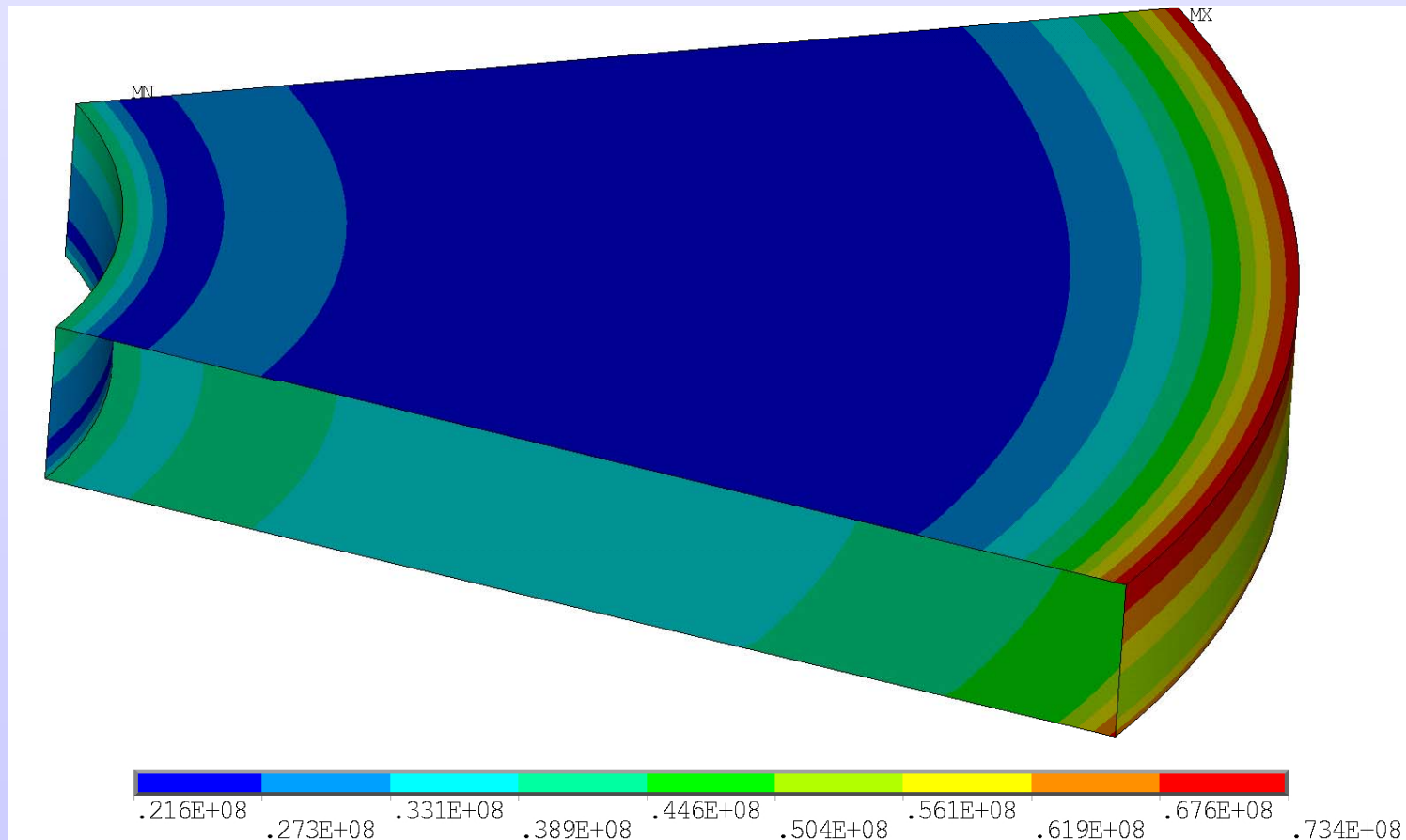


Temperature



Temperature deviation  $\pm 22\text{K}$  (against  $\pm 66\text{K}$  before)

## Tangential component of strain in SiC layer for the optimized system



## Conclusion

- **Numerical simulation is an effective tool for the design and control of induction melting and heating processes**
- **2D and 3D numerical models help to analyse, to investigate and to optimize induction melting and heating systems and processes**
- **Mathematical optimization in combination with numerical models can reduce time and costs to find the optimal design or control of an induction heating process**

## Future challenges

- **Faster calculation of complex turbulent electromagnetic driven flow fields**
- **Coupled electromagnetic and flow fields taking into account the dynamic of the melt free surface**
- **Simulation of melt flow including crystallization or solidification process at solid-liquid interfaces**
- **Simulation of 3D coupled electromagnetic-thermal processes with consideration of the field and temperature dependent permeability**
- **Simulation of stress and of material conversion during and after cooling of work-pieces like for surface hardening**
- **Development of simulation tools using OpenFOAM**

**Thank you for your attention !**